

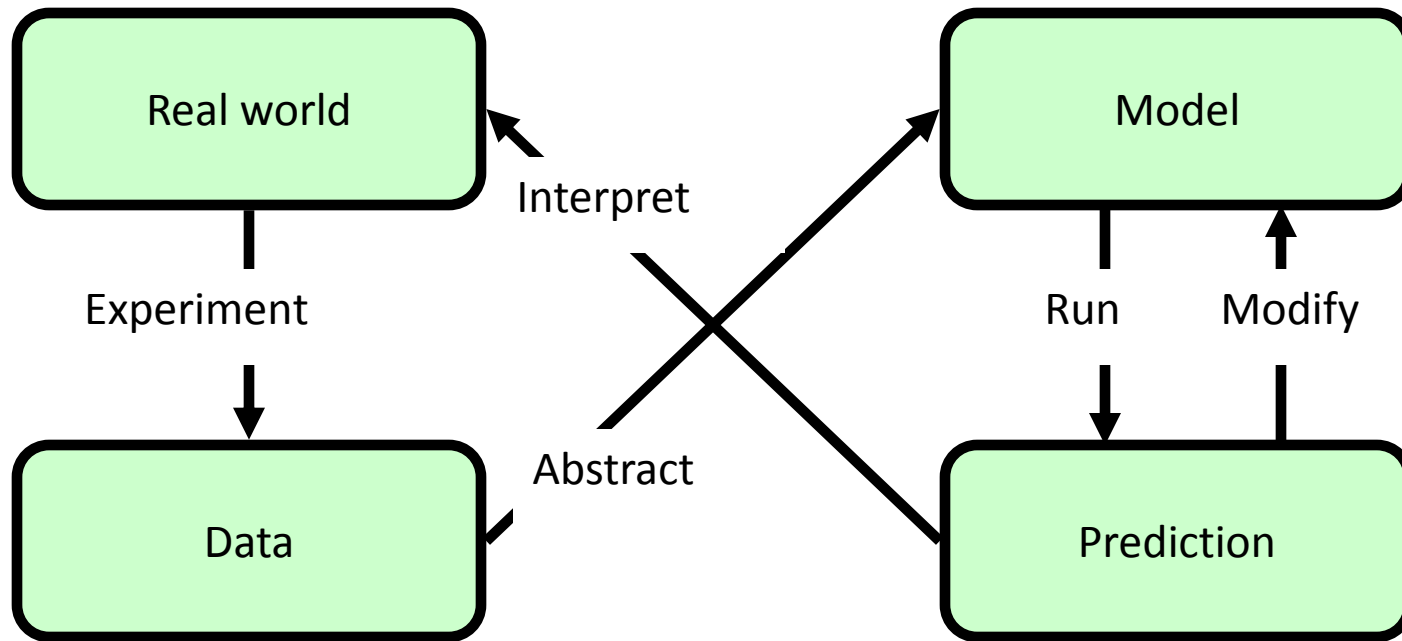
# Notes on teaching ACT-R modeling

Bill Kennedy

George Mason University

September 2011

# Why Model?



# Why Model?

1. Explain (very distinct from predict)
2. Guide data collection
3. Illuminate core dynamics
4. Suggest dynamical analogies
5. Discover new questions
6. Promote a scientific habit of mind
7. Bound outcomes to plausible ranges
8. Illuminate core uncertainties
9. Offer crisis options in near-real time
10. Demonstrate tradeoffs / suggest efficiencies
11. Challenge the robustness of prevailing theory through perturbations
12. Expose prevailing wisdom as incompatible with available data
13. Train practitioners
14. Discipline the policy dialogue
15. Educate the general public
16. Reveal the apparently simple (complex) to be complex (simple)

# Cognitive Science

- An interdisciplinary field including parts of Anthropology, Artificial Intelligence, Education, Linguistics, Neuroscience, Philosophy, and Psychology
- Goal: understanding the nature of the human mind

# Goals of AI & Cog Sci

**Artificial Intelligence:** “scientific understanding of the mechanisms underlying thought and intelligent behavior and their embodiment in machines” (from AAI website):

*demonstrated by functionality*

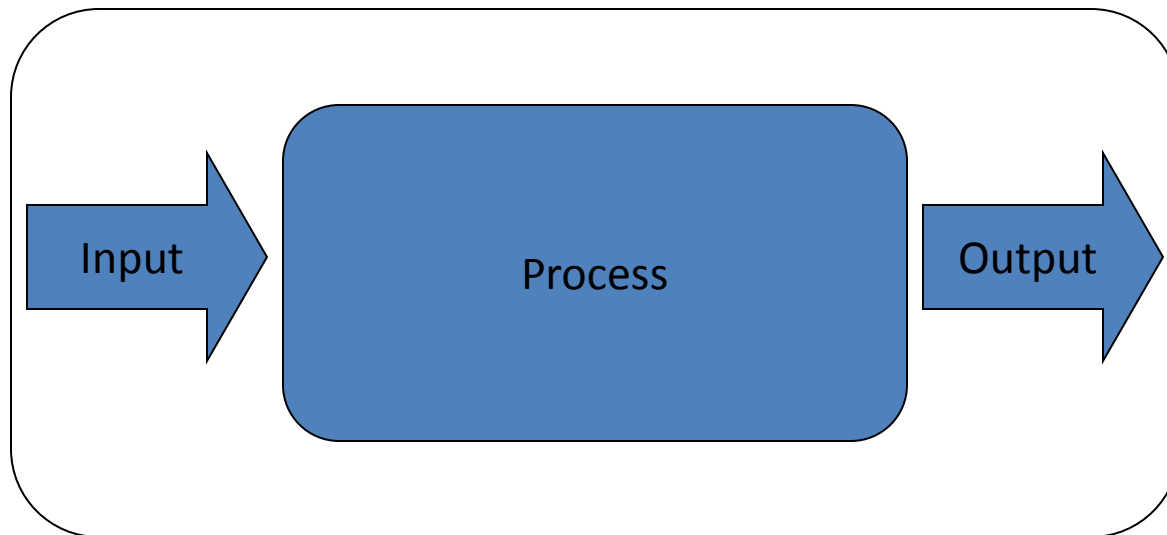
**Cognitive Science:** understanding the nature of the human mind  
*as demonstrated by models that match human behavior: i.e., matching human behavior*

# What is it?

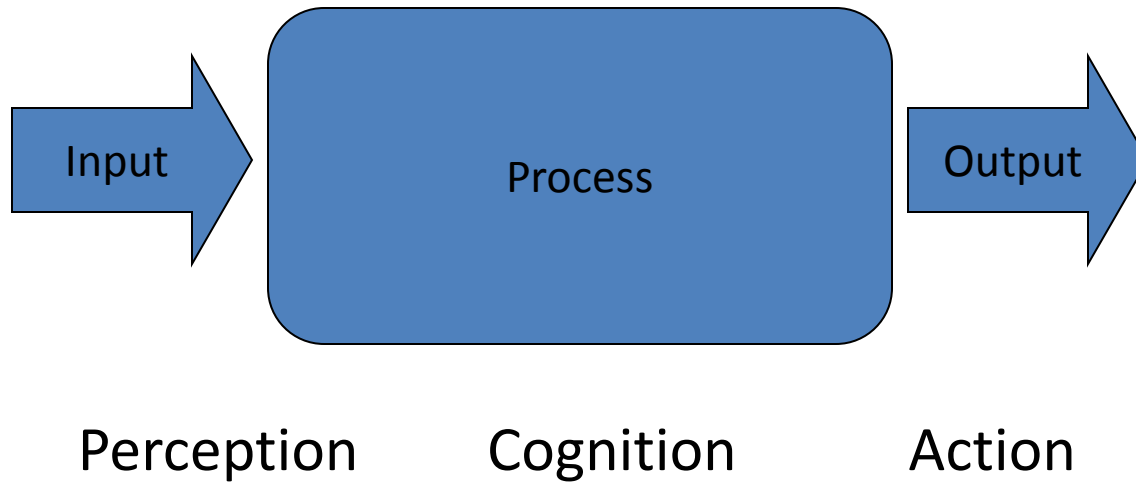


System

# What is it?

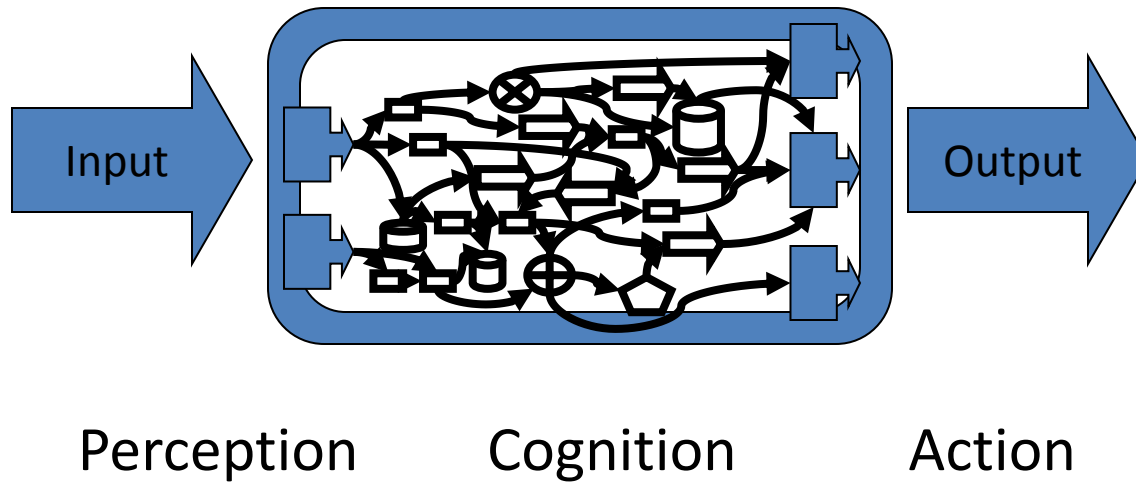


# What is it?





# What is it?



# Components

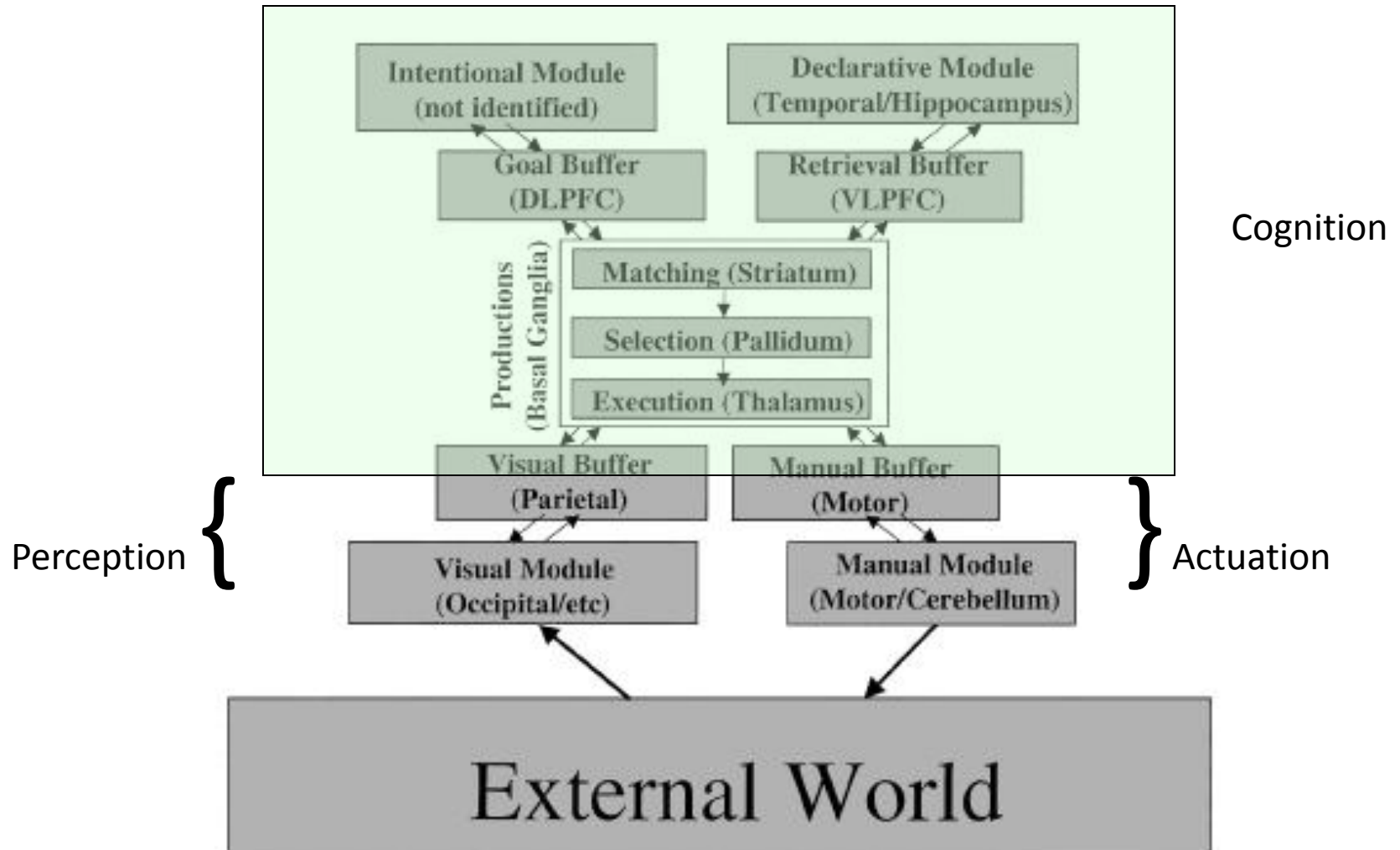
- An **architecture** is the fixed\* part of a system that implements the mind functions
- Associated with an architecture, a **model** is the variable\* part of a the mind's processing

-----

- System's knowledge representation is on the edge between architectures and models

\* with respect to a time scale (from Newell's 1990 UTC)

# ACT-R Architecture



# ACT-R Architecture Overview

- Procedure core
- Buffers
- Modules
- 2 types of knowledge representation:
  - declarative (facts, “chunks”)
  - procedural (deductions, “productions”)

# Productions

- Procedural knowledge as if-then statements
- Basic process is: match, select, fire
- Many may match current status
- Only 1 selected to fire

# Productions

- Productions use buffers in IF & THEN parts
- IF part checks buffer contents or status
- THEN part, changes buffer values or requests buffer/module action

# Productions

- Useful to translate English to ACT-R
- eg: IF the goal is to count to  $y$  AND currently at  $x$ , AND  $x < > y$ , THEN remember what comes after  $x$ .

# Production Design

- eg 1: IF the goal is to count to  $y$  AND currently at  $x$ , AND  $x < y$ , THEN remember what comes after  $x$ .
- but:
  - this production will always match and fire...
  - another production will deal with the remembered fact
  - it can work with addition of a “state” variable



# Production Design

- IF the goal is to count to y AND currently at x, AND  $x <> y$ , THEN remember what comes after y.

```
(p rule-getnext
=goal>
  isa      count
  to       y
  current  x
  - current y
  - state  recalling-next
==>
+retrieval>
  isa      next-fact
  current  x
=goal>
  state    recalling-next
)
```

count chunk type: to <n> current <m> state <w>
---

# Production Design 2

- eg 1: IF the goal is to count to  $y$  AND currently at  $x$ , AND  $x < y$ , THEN recall what comes after  $y$ .
- eg 2: IF the goal is to count with current =  $x$  AND “to” is not  $x$ , THEN recall what comes after  $x$
- eg 3: IF the goal is to count with current is  $x$  AND “to” is not  $x$ , and we remembered  $y$  comes after  $x$ , THEN update current to  $y$  and recall what comes after  $y$

# Production Design (core)

(P increment

=goal>

ISA count-from

count =num1

- end =num1

=retrieval>

ISA count-order

first =num1

second =num2

==>

=goal>

count =num2

+retrieval>

ISA count-order

first =num2

!output! (=num1)

)

count-from chunk type:

end <n>

count <m>

count-order chunk type:

first <n>

second <m>

# Production Design (start)

```
(P start
  =goal>
    ISA    count-from
    start  =num1
    count  nil
==>
  =goal>
    count  =num1
+retrieval>
  ISA    count-order
  first  =num1
)
```

# Production Design (stop)

```
(P stop
  =goal>
  ISA    count-from
  count  =num
  end    =num
==>
  -goal>
  !output!  (=num)
)
```

# ACT-R & Lisp...

- ACT-R written in Lisp
- ACT-R uses Lisp syntax
- Parts of a model
  - Lisp code (~)
  - Parameters
  - Initialization of memory (declarative & proc)
  - Running a model

# ACT-R & Lisp...syntax

- ; comments
- “(“ <function-name> <arguments> “)”  
eg: (clear-all)  
    (sgp) <= lists all parameters & settings  
    (p ... ) <= p function creates productions

# ACT-R & Lisp...warnings/errors

- Lisp warnings

```
#|Warning: Creating chunk BUZZ of default type chunk |#
```

**Undefined term, usually insignificant**

```
#|Warning: Invalid chunk definition: (RED  
                                     ISA  
                                     CHUNK) names a  
chunk which already exists. |#
```

**Some terms defined within ACT-R as chunks (~reserved words)**



# ACT-R & Lisp...warnings/errors

- Lisp /ACT-R error example 1:

```
> (help)
```

```
UNDEFINED-FUNCTION
```

```
Error executing command: "(help)":
```

```
Error:attempt to call `HELP' which is an undefined  
function..
```

Non-existent function call

# ACT-R & Lisp...warnings/errors

- Lisp /ACT-R error example 2:

```
Error Reloading:
```

```
; loading
```

```
; c:\documents and settings\bill  
kennedy\desktop\psyc-768-s09\demo2.txt
```

```
error reloading model
```

```
error:eof encountered on stream
```

```
#<file-simple-stream
```

```
  #p"c:\\documents and settings\\bill  
kennedy\\desktop\\psyc-768-s09\\demo2.txt" closed
```

```
@ #x20b2159a>
```

Unbalanced parentheses.

# ACT-R Model (outline)

```
; header info
(clear-all)
(define-model <model name>
  (sgp :<parm name> <value> <parm name> <value> ... )
  (chunk-type <isa name> <att1> <att2> ...)
  (add-dm
    (<name> isa <chunk-type> <attn> <value>
      <attn> <value> ...)
    (<name> isa <chunk-type> <attn> <value>
      <attn> <value> ...)
    ...
  ) ; end of add-dm
  (p ... )
  (goal-focus <chunk-name>)
) ; end of model definition
```

# ACT-R Model

```
(p <production name>
  =goal>
    ISA <chunk-type>
    <att> <value>
    ...
  =retrieval>           ← buffer (content)
    ISA <chunk-type>
  ?retrieval>          ← buffer (status)
    state full
==>
  =goal>
    <att> <value>
  +retrieval>          ← request to a module
    ISA <chunk-type>
    <att> <value>
    ...
  -goal>               ← explicit clearing of a buffer
  !output! (text text =variable text =variable)
)
```

# Homework: Data Fitting

- From now on the assignments will be compared to human performance
  - Mostly Response time
    - Correlation and Mean deviation
- Provides a way to compare and judge the models
- Not the only way!
  - Plausibility
  - Generality
  - Simplicity
- Make sure the model does the right thing before trying to tune it with parameters!

# Subitizing

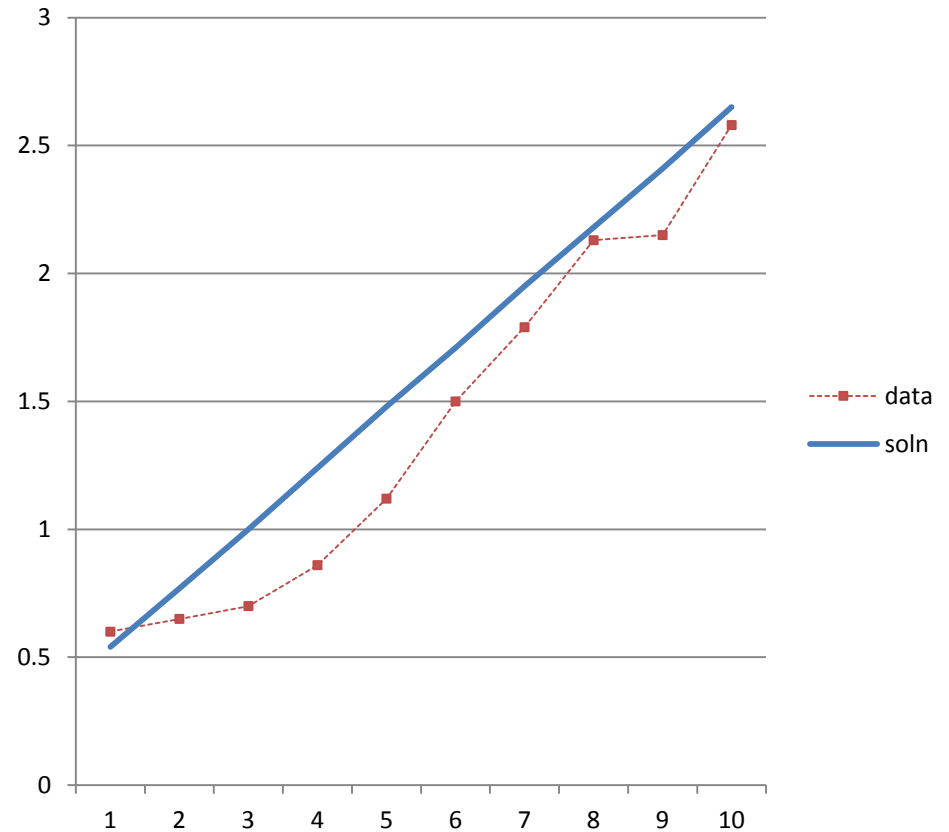
- Task: A bunch of objects appear on the display, report the number by speaking it
- Model starts with the counting facts from 0-11
- Will need to manage visual attention
  - Make sure the model gets to every item
  - Needs to know when its done
  - Given 10 finsts with a long duration to start
    - Do not have to use that if you do not want to
- Should not need to adjust parameters to get a reasonable fit to the data

# Solution Model

CORRELATION: 0.980

MEAN DEVIATION: 0.230

Items	Current	Original
1	0.54 (T )	0.60
2	0.77 (T )	0.65
3	1.00 (T )	0.70
4	1.24 (T )	0.86
5	1.48 (T )	1.12
6	1.71 (T )	1.50
7	1.95 (T )	1.79
8	2.18 (T )	2.13
9	2.41 (T )	2.15
10	2.65 (T )	2.58



# Mechanism

- Find, attend, count, repeat
- Linear in the number of items
- Any other solutions?



# Memory's Subsymbolic Representation

# Memory's Subsymbolic Representation

- At symbolic level
  - chunks in DM
  - retrieval process

```
(p add-ones
=goal>
  isa      add-pair
  one-ans  busy
  one1     =num1
  one2     =num2
=retrieval>
  isa      addition-fact
  addend1  =num1
  addend2  =num2
  sum      =sum
==>
=goal>
  one-ans  =sum
  carry    busy
+retrieval>
  isa      addition-fact
  addend1  10
  sum      =sum
)
```

- When turned on, :esc t,
  - retrieval based on chunk's "activation"

# Memory's Subsymbolic Representation: Activation

- Activation drives both latency and probability of retrieval

- Activation for chunk  $i$ :

$$A_i = B_i + \epsilon_i$$

- Retrieved \*if\* activation above a threshold (retrieval threshold :rt default 0, often -1)
- Latency calculated from activation

# Memory's Subsymbolic Representation: Activation

Activation for chunk  $i$ :

$$A_i = B_i + \varepsilon_i$$

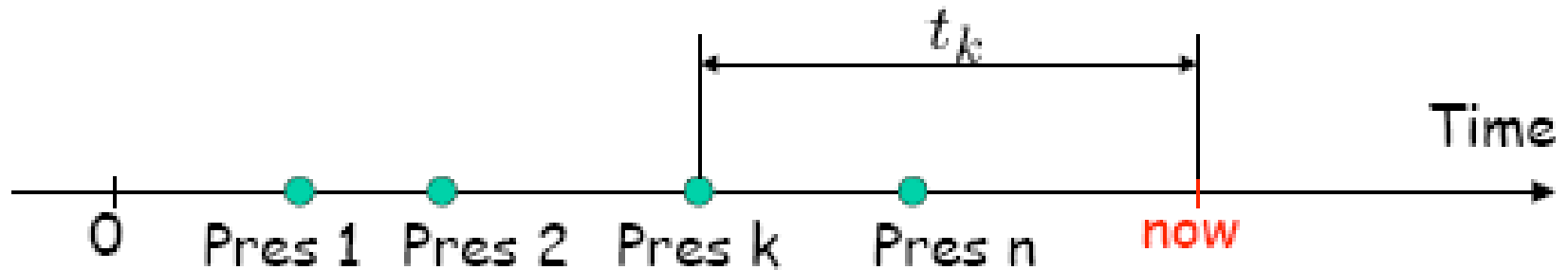
$B_i$  = “Base-level activation”

$\varepsilon_i$  = noise contribution

# Memory's Subsymbolic Representation: Base-level Activation

- Base-level activation
  - Depends on two factors of the history of usage of the chunk: recency & frequency
  - represented as the log of odds of need (Anderson & Schooler, 1991)
  - due to math representation, can be negative
  - includes every previous use
  - affected most by most recent use

# Memory's Subsymbolic Representation: Base-level Activation



$$B_i = \ln \left( \sum_k^n t_k^{-d} \right)$$

$t_k$

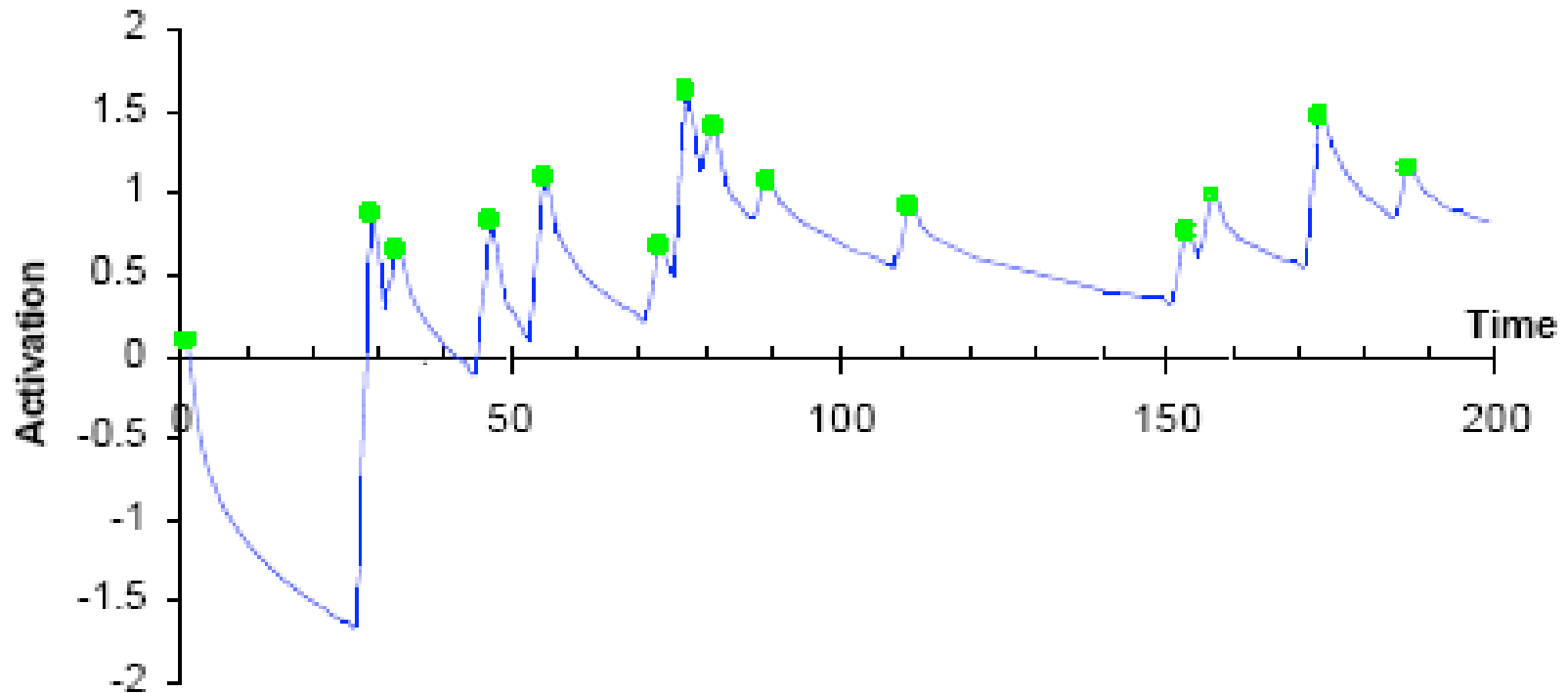
time since the k-th  
presentation of  
the chunk  $i$

$d$

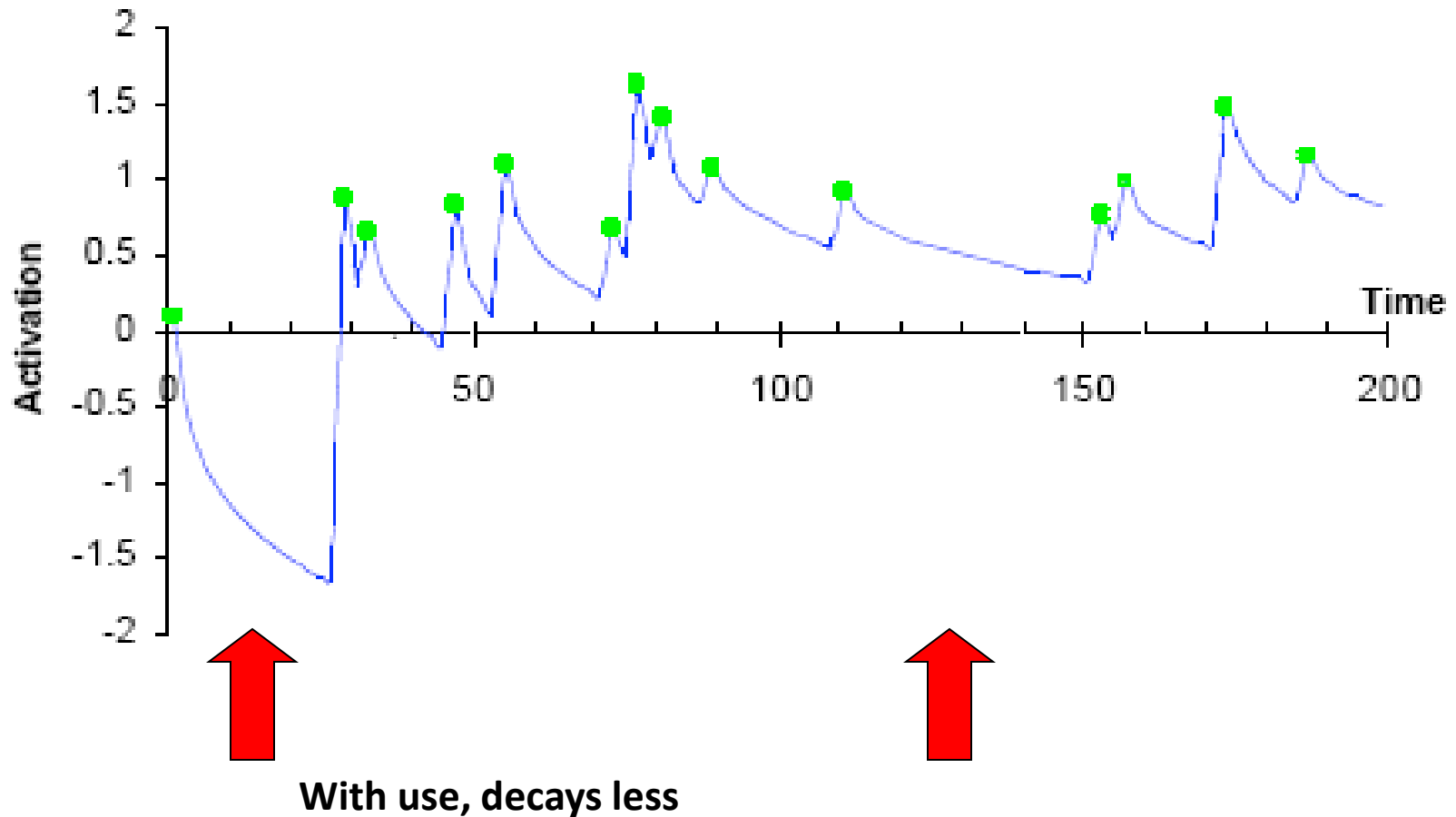
decay parameter  
(sgp :bill 0.5)

Mathematically transform the  
ages to compute the current  
strength of a memory

# Memory's Subsymbolic Representation: Base-level Activation



# Memory's Subsymbolic Representation: Base-level Activation





# Memory's Subsymbolic Representation: Base-level Activation

- Chunk events affecting activation (“event presentations”)
  - chunk creation
  - cleared from a buffer and entered into DM
  - cleared from a buffer and already in DM
  - retrieved from DM (credited when cleared)

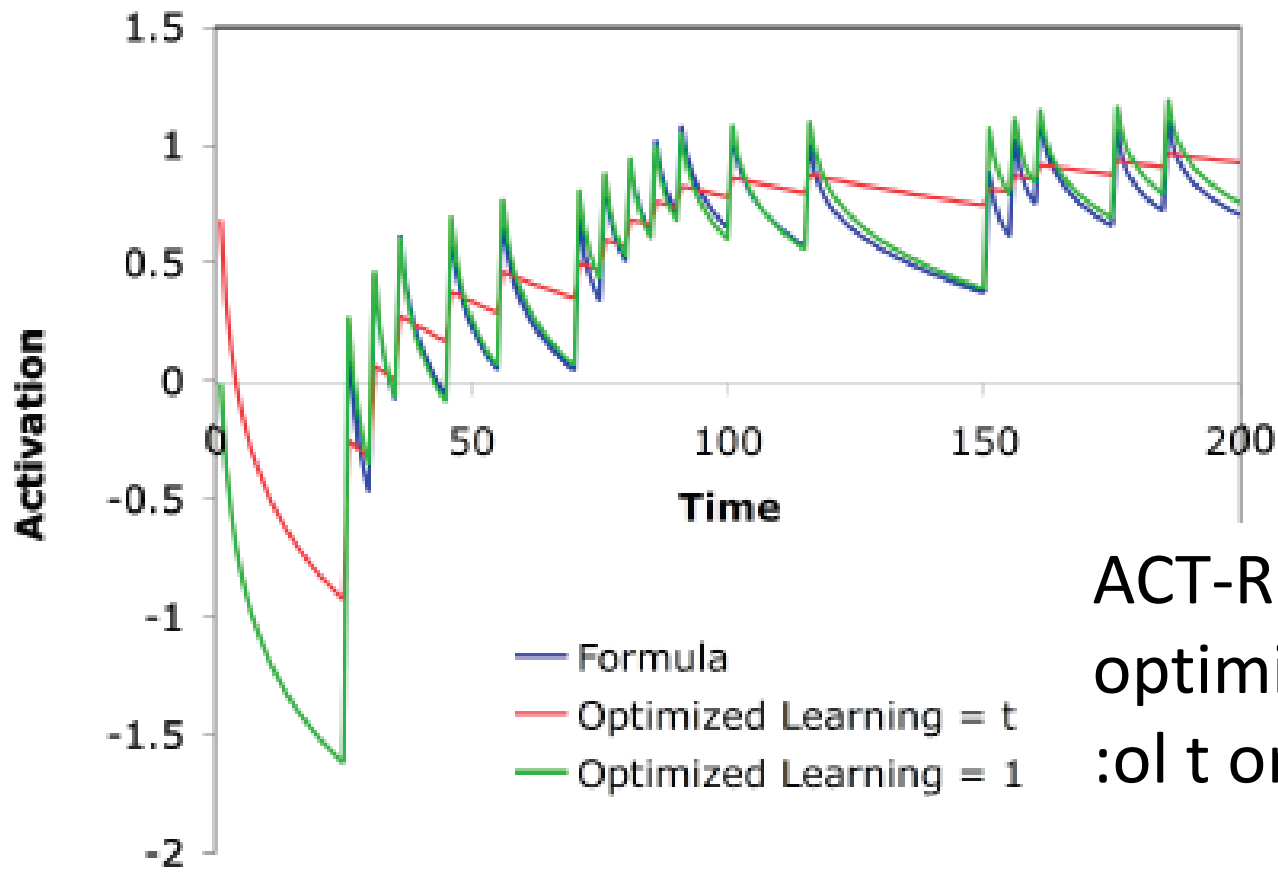
# Memory's Subsymbolic Representation: Base-level Activation

- Base-level activation calculation called “Base-Level Learning”
- Key parameter, :bll
  - the exponent in the formula
  - normal value: a half, i.e., 0.5

# Memory's Subsymbolic Representation: Base-level Activation

- Full representation requires keeping data on every previous use...
- Alternate: “Optimized” Learning
- If previous chunk events are evenly spaced, a simpler formula is possible
- Keeping even 1 previous event is effective

# Memory's Subsymbolic Representation: Base-level Activation



ACT-R parameter  
optimized learning:  
:ol t or :ol 1

# Memory's Subsymbolic Representation: Activation

Activation for chunk  $i$ :

$$A_i = B_i + \varepsilon_i$$

$B_i$  = “Base-level activation”

$\varepsilon_i$  = noise contribution

# Memory's Subsymbolic Representation: Activation Noise

- $\epsilon_i$  = noise contribution
- 2 parts: permanent & instantaneous
- both ACT-R parameters :pas & :ans
- usually only adjust :ans
- :ans setting varies, from 0.1 to 0.7
- noise in model sometimes nec'y to match noise of human subjects...

# Memory's Subsymbolic Representation: Latency(s)

- Activation also affects latency (two ways)
- Latency =  $F * e^{-A}$ 
  - A is activation
  - F is “latency factor” (ACT-R parameter :lf ~0.5)
- Threshold setting affects latency of retrieval failure
  - (must wait until latency of threshold passes!)

# Memory's Subsymbolic Representation

- Activation = base-level and noise
- Base-level dependent of recency & frequency of previous chunk “presentations”
- Retrieval only when activation above “retrieval threshold”
- Activation and threshold affect latency
- Many parameters :esc, :rt, :bll, :ol, :ans



# Memory II:

## Other Sources of Activation

- Previously, chunk's activation over time
- Now, add the effect of context (two types)

# Other Sources: Spreading Activation & Partial Matching

- Activation (previous):

$$\begin{aligned} A_i &= \text{Base Level Activation} + \text{noise} \\ &= B_i + \varepsilon_i \end{aligned}$$

- the effect of context (new):

$$A_i = B_i + \varepsilon_i + SA + PM$$

# Spreading Activation

- Learn multiple similar facts, e.g.,

A hippie is in the park

A lawyer is in the cave

A debutante is in the bank

A hippie is in the cave

A lawyer is in the church

# Spreading Activation

- Tests (seen before Y/N?)

A lawyer is in the park

A hippie is in the cave

# Spreading Activation

- Responses time increases linearly as number of persons and locations increase, i.e., “fanning out” of activation
- Foils take longer than targets to decide

# Spreading Activation

- The context affects retrievals
- Contents of other buffers contribute to retrieval activation calculation for chunks in DM
- Affects response time

# Spreading Activation

- Consider: several matching chunks in memory
- How decide which?
- Activation based on base (recency & frequency) PLUS small context effect
- Retrieval based on parts of chunk separates exact matches from non-matches

# Spreading Activation

- Activation (previous):

$$\begin{aligned} A_i &= \text{Base Level Activation} + \text{noise} \\ &= B_i + \varepsilon_i \end{aligned}$$

- add context: effect of other buffers' chunks

$$A_i = B_i + \varepsilon_i + \sum_{\text{buffers}(k)} \sum_{\text{slots}(j)} (W_{kj} S_{ji})$$



# Spreading Activation

- add context: effect of other buffers' chunks

$$A_i = B_i + \epsilon_i + \sum_{\text{buffers}(k)} \sum_{\text{slots}(j)} (W_{kj} S_{ji})$$

$W_{kj}$  is weighting of slot  $j$  in buffer  $k$  (normalized)

$S_{ji}$  is the strength of the association between  
slot  $j$  and chunk  $i$

# Spreading Activation

- add context: effect of other buffers' chunks

$$A_i = B_i + \epsilon_i + \sum_{\text{buffers}(k)} \sum_{\text{slots}(j)} (W_{kj} S_{ji})$$

$W_{kj}$  is weighting of slot  $j$  in buffer  $k$  (normalized)  
(default is 1 for goal, 0 for others)

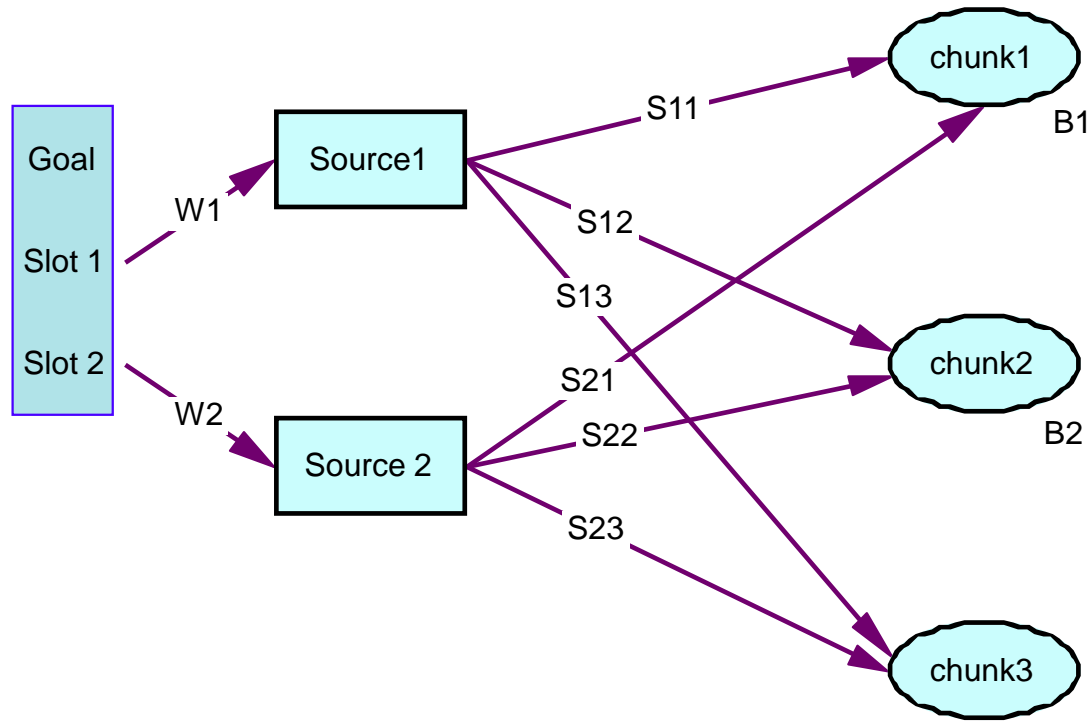
$S_{ji}$  is the strength of the association between  
slot  $j$  and chunk  $i$  ( $S_{ji}=0$  or  $S-\ln(\text{fan}_j)$  )

# Spreading Activation

## Fan Effect (Anderson 1974)

- Fan effect: number of associations “fanning out” from a chunk
- Other buffers hold chunks
- Chunk has slots with other chunks
- How many uses of a chunk affects its  $A_i$

# Spreading Activation: Fan Effect



$$A_1 = B_1 + W_1 S_{11} + W_2 S_{21}$$
$$A_2 = B_2 + W_1 S_{12} + W_2 S_{22}$$
$$A_3 = B_3 + W_1 S_{13} + W_2 S_{23}$$

# Spreading Activation: Fan Effect

- Retrievals based on matching & activation
- Now, other buffers affect retrieval
- But, activation diluted by similar chunks
- Effect:  
Similar but non-matches slow retrievals

# Other Sources: Partial Matching

# Other Sources: Partial Matching

- Provides ACT-R a mechanism to explain errors of commission, retrieving wrong chunk
- (previous activation mechanism explained errors of omission,  $A_i < :RT$  )

# Partial Matching

- add context: effect of similar chunks

$$A_i = B_i + \epsilon_i + \sum_{\text{buffers}(k)} \sum_{\text{slots}(j)} (W_{kj} S_{ji}) + \sum_{\text{retrieval slots}} PM_{li}$$

P is weighting of slot

$M_{ij}$  is the similarity between values in slot  $j$  of retrieval and slot  $i$  of chunk



# Partial Matching

- add context: effect of similar chunks

$$A_i = B_i + \epsilon_i + \sum_{\text{buffers}(k)} \sum_{\text{slots}(j)} (W_{kj} S_{ji}) + \sum_{\text{retrieval slots}} PM_{li}$$

P is weighting of slots (all equal)

$M_{ij}$  is the similarity between values in slot  $j$  of retrieval and slot  $i$  of chunk

# Partial Matching

- Effect is can retrieve a wrong but similar chunk (... IF chunk hierarchy supports it)
- Retrieval of wrong chunk supports errors of commission, taking wrong action vice no action

# ACT-R Modeling

- ACT-R Model Development
- ACT-R Model Debugging

# ACT-R Model Development

1. Plan overall model to work in stages.
2. Start simple then add details to your model.
3. Write simple productions using simple chunks.
4. Run the model (with own trace) frequently to test progress (eg. with every new or changed production).

# ACT-R Model Development

5. Start with productions doing one thing at a time (i.e., reference goal + one buffer) and use multiple productions. Combine later.
6. Use state variables to rigorously control sequencing until model works, then remove as many as possible.

# ACT-R Model Development

7. With each buffer request, consider a production for handling the failure.
8. In using loops, consider preps to start and how to leave loop.

# ACT-R Debugging Process

- Run ACT-R up to problem...
  - set time limit
  - change production to stop at problem step
- Check "why not" of expected production
- Check buffers & buffer status
- Check visicon
- Causes ...

# ACT-R Code Debugging

*Stops unexpectedly/expected production not firing:*

- Conditions not met (use "Why not" to identify which)
- Conditions over-specified with unnec'y variable tests which don't match
- Logic mismatch among conditions
- nil will not match =variable
- ...



# ACT-R Code Debugging

*Stops unexpectedly/expected production not firing (continued):*

- Typo on variable name, i.e., not same ref.
- Wrong slot referenced in LHS
- Time ran out
- Production not in memory
- Error on loading (production ignored)
- Production overwritten by duplicate naming (warning)

# ACT-R Code Debugging

## *Wrong production firing:*

- Firing production also meets current conditions
- Conditions do not meet expected production LHS

## *Production firing repeatedly:*

- LHS not changed by firing, i.e., still valid

# ACT-R Code Debugging

## *Buffer unexpectedly empty:*

- Not filled
- Implicit clearing (on LHS but not RHS)

## *Buffer with unexpected chunk:*

- Previous production to fill it didn't fire
- Sensor handling not as expected
- Buffer not updated/cleared as expected

# ACT-R Code Debugging

## *Retrieval unsuccessful:*

- Expected chunk not in memory
- Retrieval specification unintended
  - overly specific (too many slots specified)
  - unintended chunk type
- Expected chunk's activation too low
- Wrong chunk retrieved
  - under specified (too few slots specified)
  - partial matching effect (intended)

# ACT-R Code Debugging

## *Timing too slow:*

- Combine productions
- Driven by retrieval failures and :RT too low

## *Timing too fast:*

- Driven by retrieval failures and :RT too high

# Unit 4: Zbrodoff's Experiment

- alpha arithmetic, eg:  $A + 2 = C$ : correct?
- possible addends: 2, 3, or 4
- learning over:
  - stimuli set (24)
  - repetition (5)
  - blocks (2) = 192 trials

# Model Design

- Given model that counts to answer
- Process: read problem, count, answer
- Already creates saves chunks of answers
- Strategy?

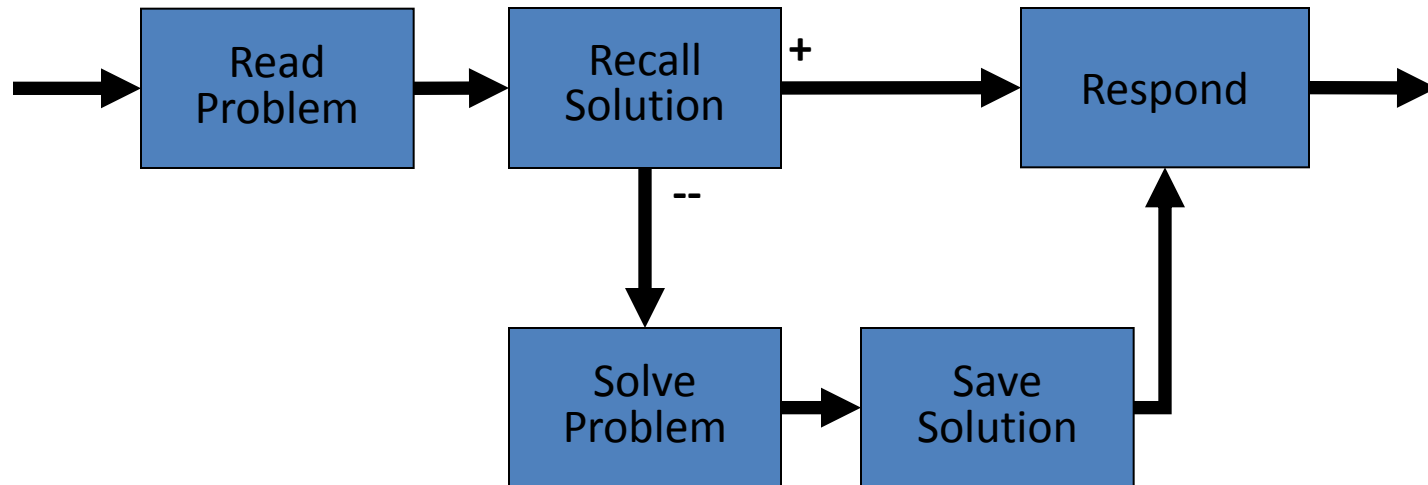
# Model Design - start

- Basic strategy: learn to retrieve answer
- How: attempt retrieval
  - if successful, answer based on it
  - if fails, resort to counting  
(another basic process...)
- After model runs, adjust :RT



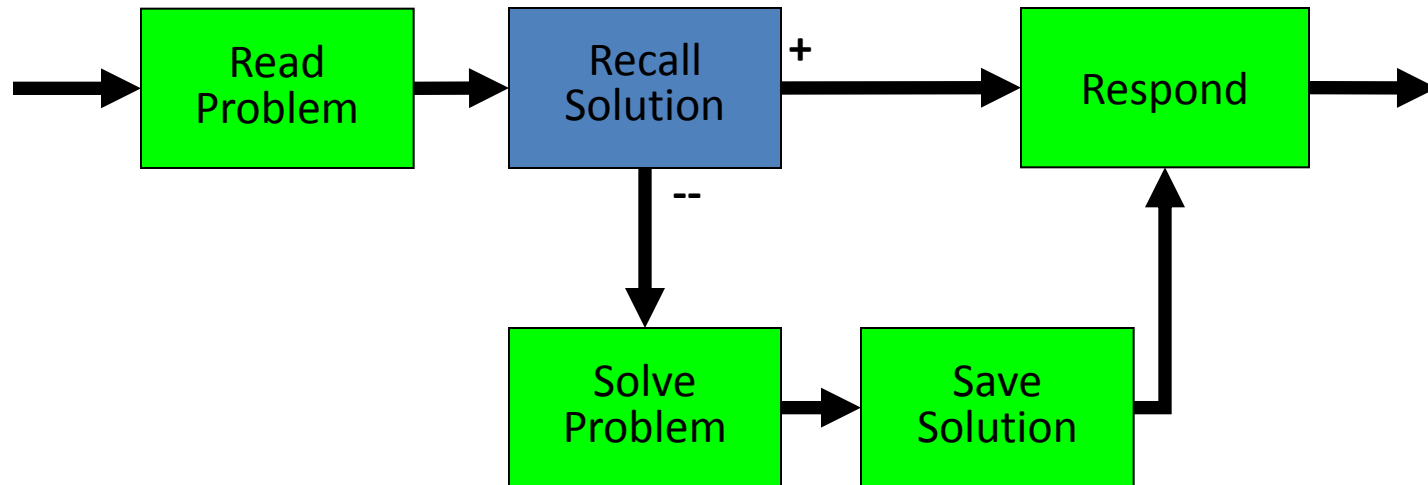
# Model Design – basic process

Instance-based action/declarative learning process:



# Model Coding

Ziegler homework: ~80% given



# Parameter Tweaking

- After model runs, adjust retrieval threshold to control when learning occurs vs. problem solving

# Unit 5: Siegler Experiment

- Experiment is 4 yr olds answering addition problems:  $1+1$  up to  $3+3$  (answers from 0-8 & “other”)
- Environment starts with problem stuffed into imaginal buffer as “text”
- Goal: beat 0.976 / 0.058
- Strategy?

# Model Development Process

1. get working for one case
2. expand for all cases
3. adjust parameters

# Model / Coding Issue

- Note: one <> “one” <> “1” <> 1,  
(symbol, strings, and a constant)
- Facts stored using different representations  
Number fact: (one ISA number value 1 name "one")  
Addition fact: (f11 ISA plus-fact addend1 one  
addend2 one sum two)
- problem input & response as strings, eg., “one”

# Model / Coding Issue

- Now possible to access to chunk names  
eg., =retrieval  
like previous =visual-location
- Or, (“old school”) add slot with value, eg:  
(four ISA number value 4 name "four" ref four)

# Model Design - basics

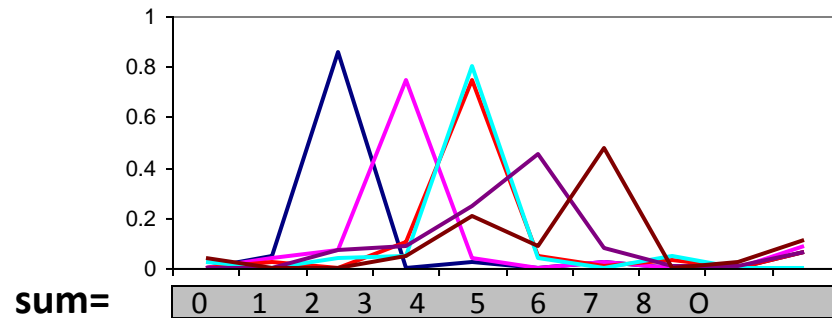
- Given chunk types and functions to set base activation and set similarities
- Basic process: encode, retrieve, respond



# Parameter Tweaking

- Set base level activations for successful retrievals throughout a run
- Adjust :ans to get “other” responses
- Set similarities to generate error distribution to match human subjects

# Siegler Experiment Data

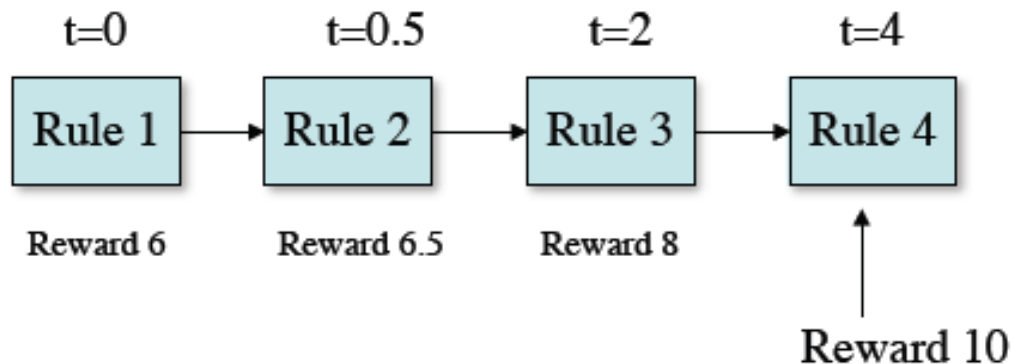


	zero	one	two	three	four	five	six	seven	eight	other
<b>1+1</b>	0	0.05	0.86	0	0.02	0	0.02	0	0	0.06
<b>1+2</b>	0	0.04	0.07	0.75	0.04	0	0.02	0	0	0.09
<b>1+3</b>	0	0.02	0	0.1	0.75	0.05	0.01	0.03	0	0.06
<b>2+2</b>	0.02	0	0.04	0.05	0.8	0.04	0	0.05	0	0
<b>2+3</b>	0	0	0.07	0.09	0.25	0.45	0.08	0.01	0.01	0.06
<b>3+3</b>	0.04	0	0	0.05	0.21	0.09	0.48	0	0.02	0.11

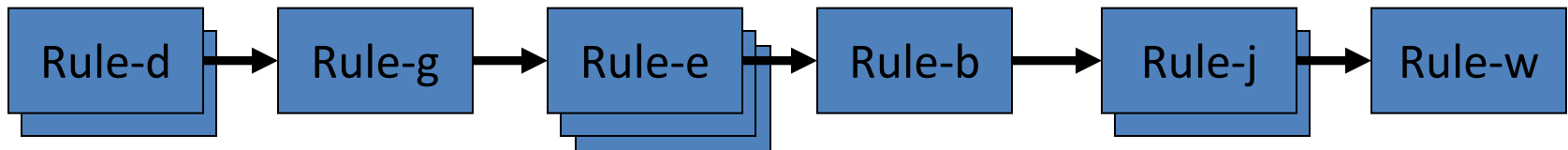


# Procedural Knowledge “Reward”

- A reward value is propagated backwards through rule firings and depreciated by time

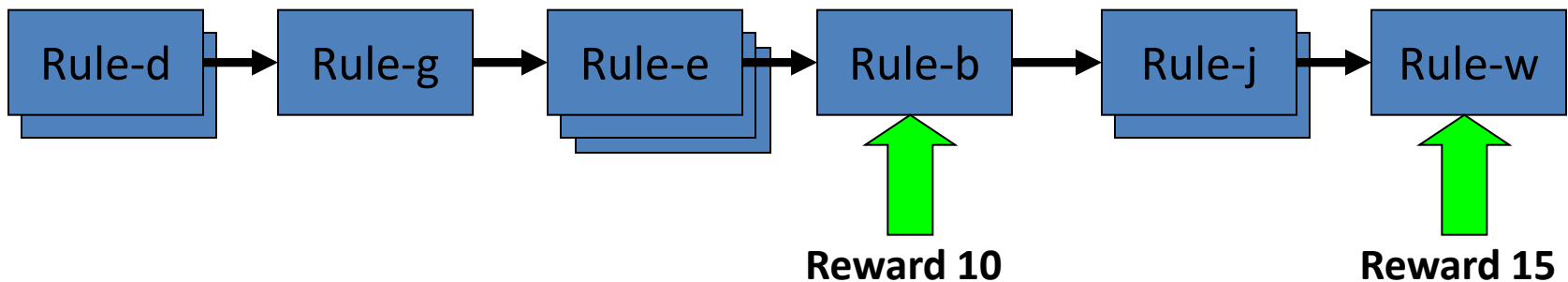


# Procedural Knowledge “Reward”



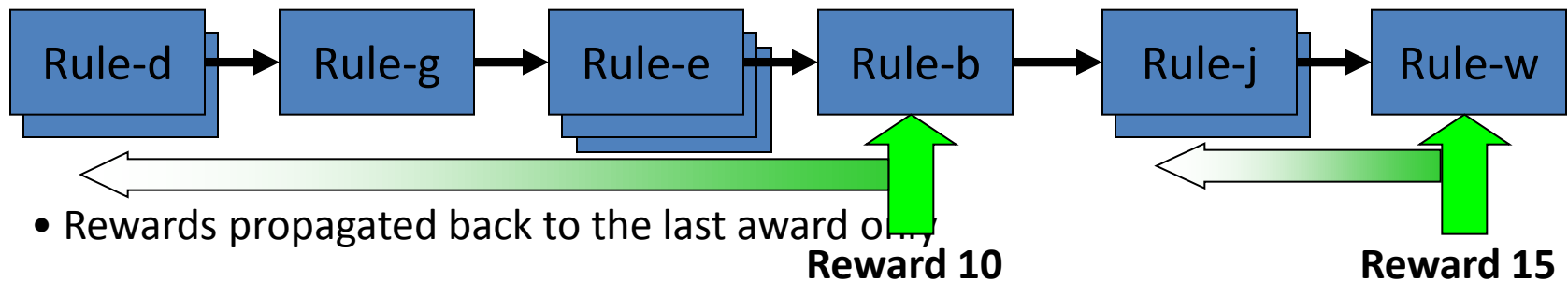
# Procedural Knowledge “Reward”

- Eg: (spp Rule-b :reward 10)  
(spp Rule-w :reward 15)



# Procedural Knowledge “Reward”

- Eg: (spp Rule-b :reward 10)  
(spp Rule-w :reward 15)



# Why?

- Multiple rules' LHS meet current conditions and appropriate strategy is a balance between the them.
- Rule selection balance can be learned
- To turn on utility learning: `(sgp :u1 t)`



# Learning Utility

- Difference Learning Equation:

$$U_i(n) = U_i(n-1) + \alpha [ R_i(n) - U_i(n-1) ]$$

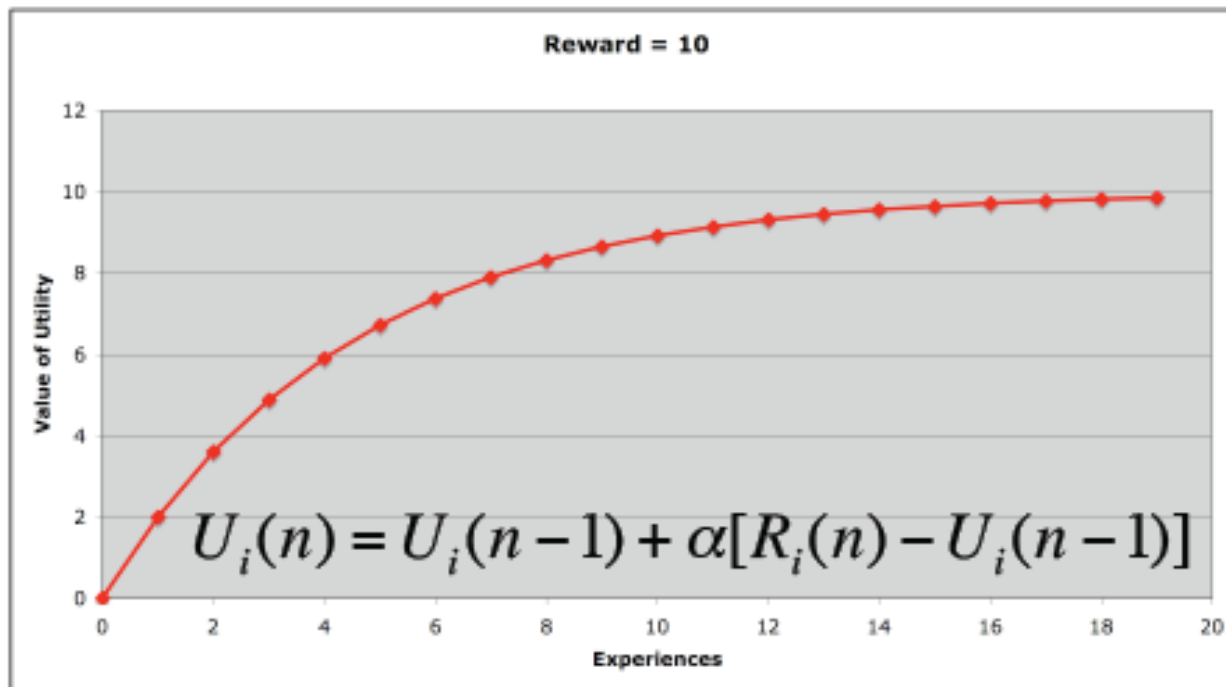
$U_i(n)$  is utility of rule  $i$  at  $n^{\text{th}}$  firing

$R_i(n)$  is reward for rule  $i$  at  $n^{\text{th}}$  firing

$\alpha$  is “learning rate”      (`sgp :alpha 0.2`)

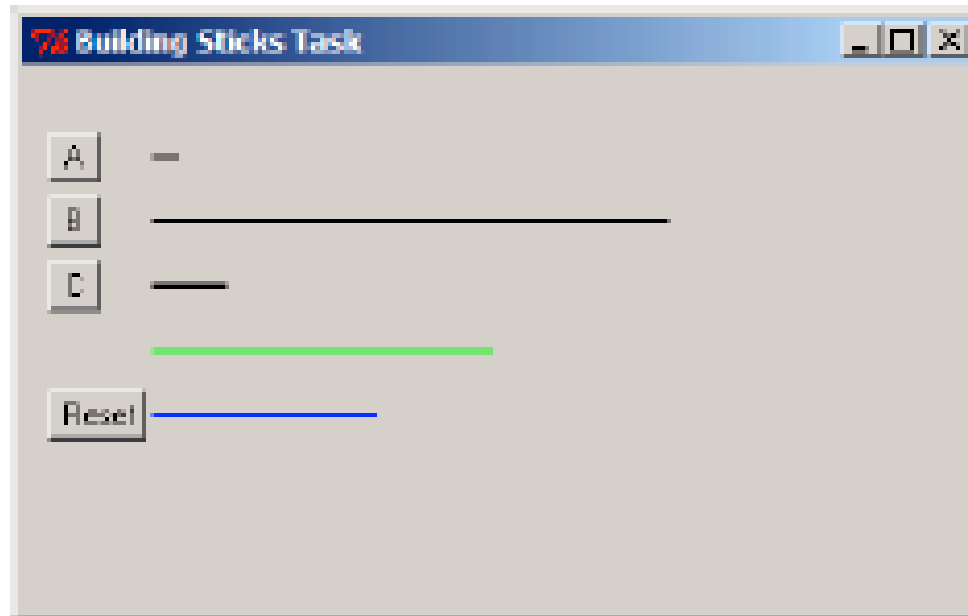
# Learning Utility

- Difference Learning Equation effect:

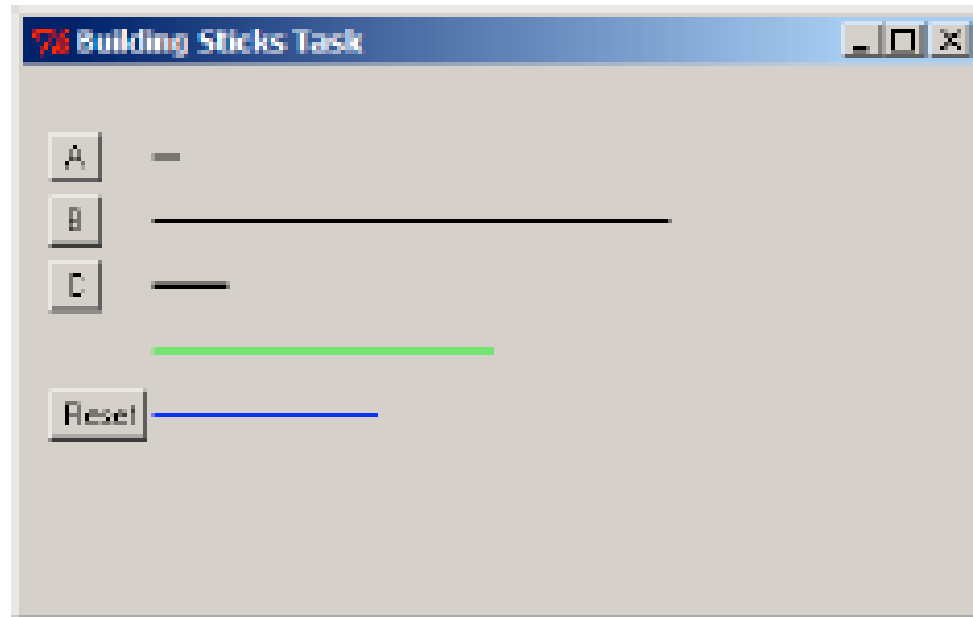


# Example: Building Sticks Task

- Match a given length by a combination of 3 other given lengths
- Two strategies: building up or subtracting (“undershoot”/“overshoot” based on first move)



# Example: Building Sticks Task



- Searching for combination of A,B, & C that equals target length (green)
- If current is too long, length is subtracted

# Example: Building Sticks Task

Demo

$A=15, B=200, C=41$

Goal: 103

# Example: Building Sticks Task

Demo

$A=15, B=200, C=41$

Goal:  $103 = B - 2C - A$

# Example: Building Sticks Task

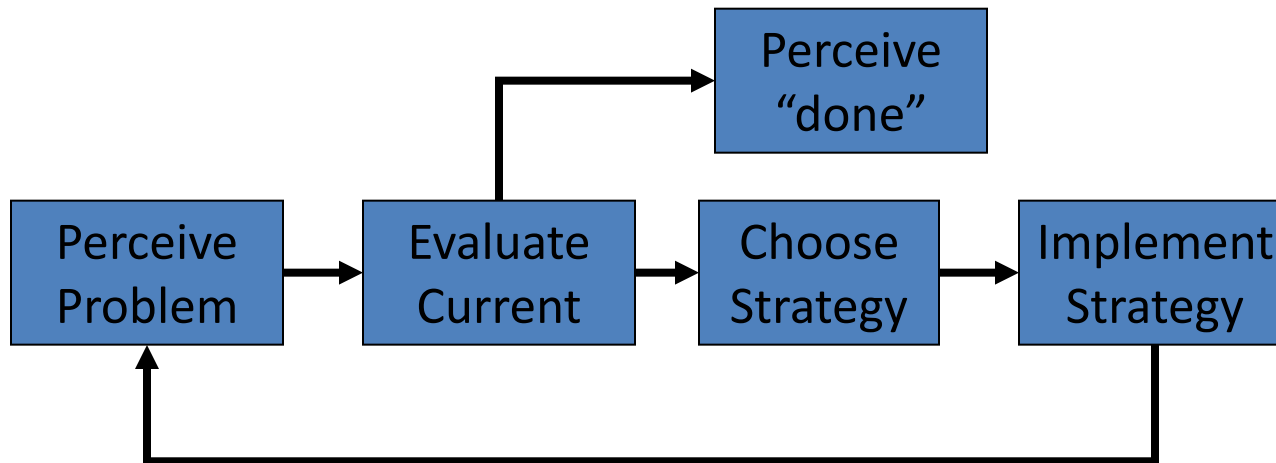
Human performance data:

available lengths			Goal	%Overshoot
a	b	c		
15	250	55	125	20
10	155	22	101	67
14	200	37	112	20
22	200	32	114	47
10	243	37	159	87

...

# Example: Building Sticks Task

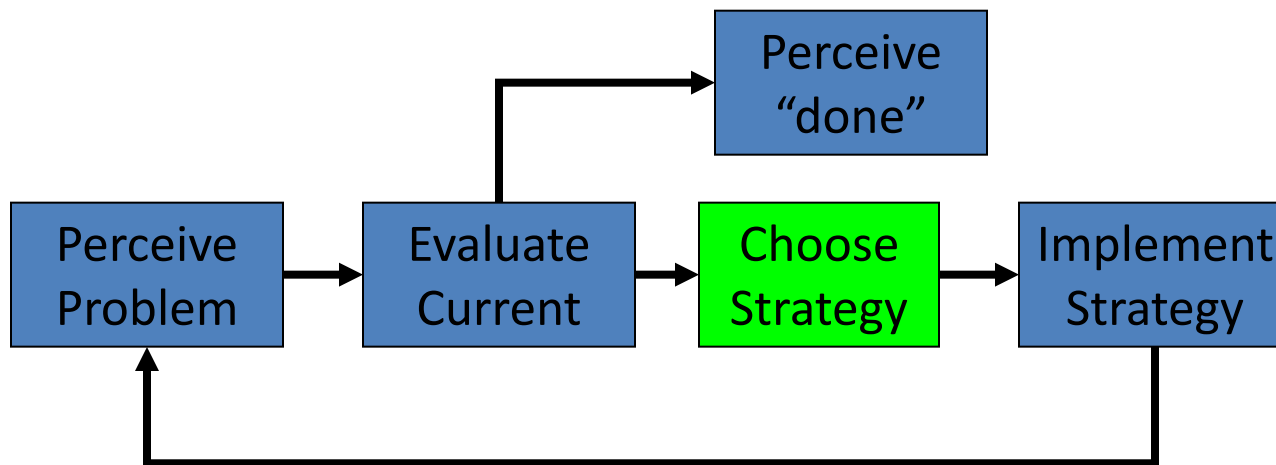
- BST model has 27 productions





# Example: Building Sticks Task

- BST model has 27 productions



# Example: Building Sticks Task

- BST model has 27 productions
- Key productions decide which length to use based on whether current length is too long (“over”) or too short (“under”)

**decide-over**

**decide-under**

**force-over**

**force-under**

# Example: Building Sticks Task

```
(p decide-under
  =goal>
    isa      try-strategy
    state    choose-strategy
    strategy nil
  =imaginal>
    isa      encoding
    over     =over
    under    =under

!eval! (< =under (- =over 25))
==>
=imaginal>
=goal>
  state    prepare-mouse
  strategy under
+visual-location>
  isa      visual-location
  kind     oval
  screen-y 85)
```

```
(p force-under
  =goal>
    isa      try-strategy
    state    choose-strategy
  - strategy under

==>
=goal>
  state    prepare-mouse
  strategy under
+visual-location>
  isa      visual-location
  kind     oval
  screen-y 85)
```

# Example: Building Sticks Task

- (collect-data 100) → corr: 0.803
- Utilities      start → end
  - decide-over      13 → 13.15
  - decide-under    13 → 11.15
  - force-over       10 → 12.15
  - force-under      10 → 6.59

# Unit 6 Homework

## Model design:

productions

- start by detecting “choose” in window
- generate key-press (heads and tails)
- read actual result
- note matches and non-matches

settings :ul t (to turn on utility learning)

:egs noise parameter

set initial utilities

AND establish rewards for specific productions

# Unit 6 Homework

Model results (collect-data 100):

Corr: / Mean Dev.

official answer:      0.991 / 0.012

# Unit 6 Homework

Model results (collect-data 100):

Corr: / Mean Dev.

official answer: 0.991 / 0.012

my best: 0.998 / 0.010

# Unit 6 Homework

Model results (collect-data 100):

Corr: / Mean Dev.

official answer: 0.991 / 0.012

my best: 0.998 / 0.010

another run: 0.990 / 0.030

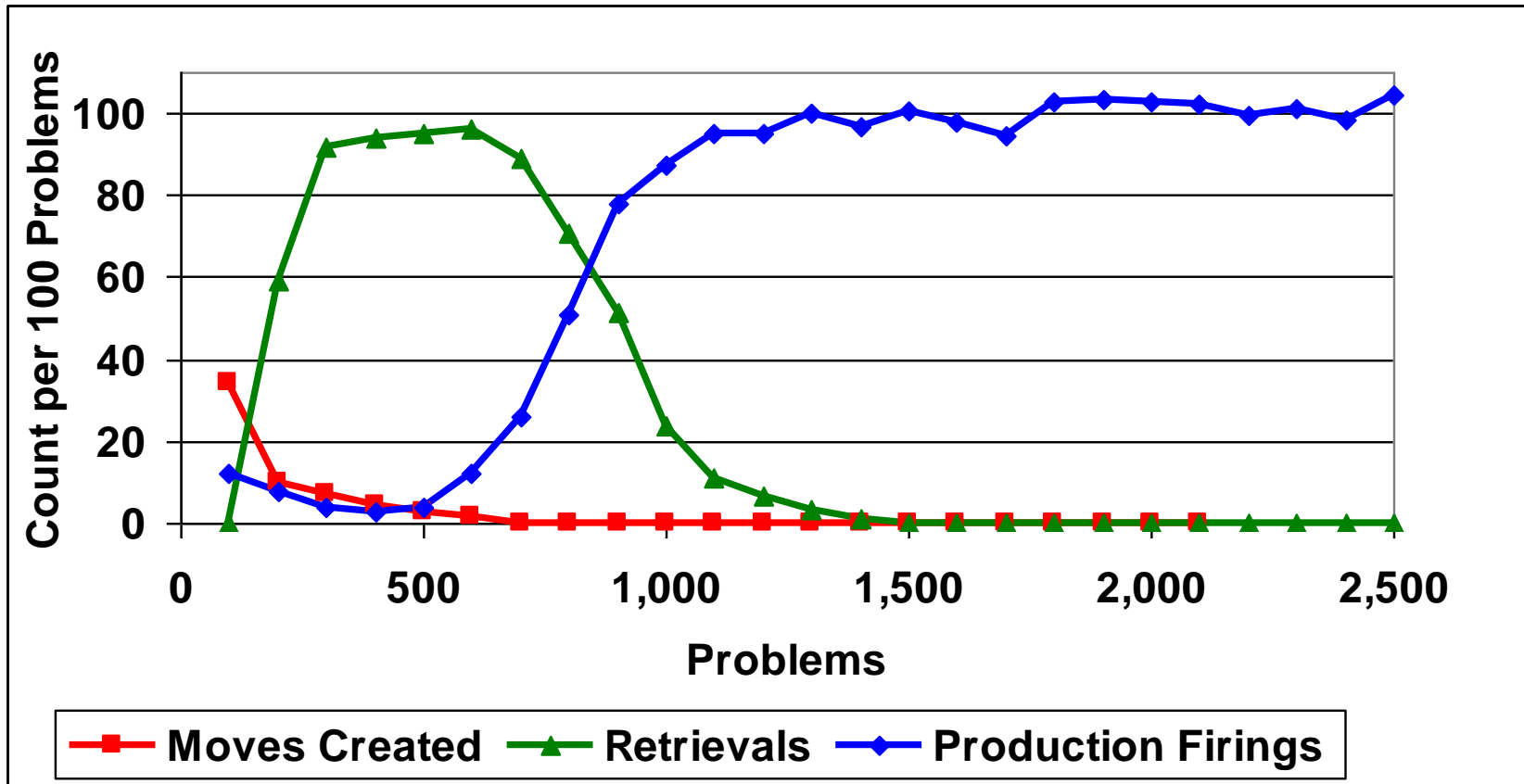
run 200: 0.990 / 0.024



# Learning New Rules

- Anderson (1982) suggested a 3 stage learning process:
  - “Cognitive” (problem solving, chunking)
  - “Associative” (retrieval of solutions)
  - “Autonomous” (new procedural knowledge)

# Learning New Rules



from Kennedy & Trafton (2007) Long-term Learning, CSR

# Learning New Rules

- How? compiling rules that fire sequentially

Abstract:

Rule  $A \rightarrow B$  followed by rule  $B \rightarrow C$

...

# Learning New Rules

- How? compiling rules that fire sequentially

Abstract:

Rule  $A \rightarrow B$  followed by rule  $B \rightarrow C$  combined into a new rule:  $A \rightarrow B \& C$

# Learning New Rules

```
(p rule1
  =goal>
  isa   goal
  state nil
==>
  =goal>
  state start
)
```

```
(p rule2
  =goal>
  isa   goal
  state start
==>
  =goal>
  add1 zero
)
```

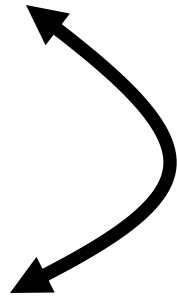
# Learning New Rules

```
(p rule1
  =goal>
  isa goal
  state nil
==>
  =goal>
  state start
)
```

A



B



```
(p rule2
  =goal>
  isa goal
  state start
==>
  =goal>
  add1 zero
)
```

B



C

# Learning New Rules

```
(p rule1  
  =goal>  
  isa goal  
  state nil
```

==>

```
  =goal>  
  state start  
)
```

```
(p rule2  
  =goal>  
  isa goal  
  state start
```

==>

```
  =goal>  
  add1 zero  
)
```

```
(p rule1+2  
  =goal>  
  state nil
```

==>

```
  =goal>  
  state start  
  add1 zero  
)
```

**A**

**→**

**B**

**C**

# Learning New Rules

```
(p rule1
  =goal>
  isa goal
  state nil
==>
  =goal>
  state start
)
```

```
(p rule2
  =goal>
  isa goal
  state start
==>
  =goal>
  add1 zero
)
```

```
(p rule1+2
  =goal>
  state nil
==>
  =goal>
  state start
  add1 zero
)
```



# Learning New Rules

- Is that all?

Realistic example:

- Rule 1 initiates retrieval of a chunk
- Rule 2 harvests the retrieved chunk
- New Rule 1+2 built with chunk information  
“built in” i.e., no retrieval involved

# Learning New Rules

Realistic example (specifics):

- Recall the two column addition exercise
- Add by counting from first number, the second number of times
- Consider a specific case: start with 3 and need to count 2 steps to get sum

# Learning New Rules

```
(P initialize-add-count
=goal>
  ISA      add
  addend1  =arg1
  addend2  =arg2
  sum      nil
```

==>

```
+retrieval>
  ISA      order
  first    =arg1
=goal>
  sum      =arg1
  count    zero
```

```
(P increment-sum
=goal>
  ISA      add
  sum      =sum
  count    =count
=retrieval>
```

```
  ISA      order
  first    =sum
  second   =new
```

==>

```
=goal>
  sum      =new
+retrieval>
  ISA      order
  first    =count
```

# Learning New Rules

```
(P initialize-add-count
=goal>
  ISA      add
  addend1  =arg1
  addend2  =arg2
  sum      nil
```

==>

```
+retrieval>
  ISA      order
  first    =arg1
=goal>
  sum      =arg1
  count    zero
```

```
(P increment-sum
=goal>
  ISA      add
  sum      =sum
  count    =count
=retrieval>
```

```
  ISA      order
  first    =sum
  second   =new
```

==>

```
=goal>
  sum      =new
+retrieval>
  ISA      order
  first    =count
```

Retrieved chunk:

```
ISA      order
first    three
second   four
```

# Learning New Rules

```
(P initialize-add-count
=goal>
ISA      add
addend1  =arg1
addend2  =arg2
sum      nil
```

==>

```
+retrieval>
ISA      order
first    =arg1
=goal>
sum      =arg1
count    zero
```

```
(P increment-sum
=goal>
ISA      add
sum      =sum
count    =count
=retrieval>
```

```
ISA      order
first    =sum
second   =new
```

==>

```
=goal>
sum      =new
+retrieval>
ISA      order
first    =count
```

Retrieved chunk:

```
ISA      order
first    three
second   four
```

# Learning New Rules

```
(P initialize-add-count
=goal>
ISA      add
addend1  =arg1
addend2  =arg2
sum      nil
```

==>

```
+retrieval>
ISA      order
first    =arg1
=goal>
sum      =arg1
count    zero
```

```
(P increment-sum
=goal>
ISA      add
sum      =sum
count    =count
=retrieval>
```

```
ISA      order
first    =sum
second   =new
```

==>

```
=goal>
sum      =new
+retrieval>
ISA      order
first    =count
```

Retrieved chunk:

ISA	order
first	three
second	four

# Learning New Rules

```
(P initialize-add-count
=goal>
ISA      add
addend1  three
addend2  =arg2
sum      nil
```

==>

```
+retrieval>
ISA      order
first    three
=goal>
sum      three
count    zero
```

```
(P increment-sum
=goal>
ISA      add
sum      three
count    =count
```

=retrieval>

```
ISA      order
first    three
second   four
```

==>

```
=goal>
sum      four
+retrieval>
ISA      order
first    =count
```

Retrieved chunk:

```
ISA      order
first    three
second   four
```

# Learning New Rules

```
(P initialize-add-count
=goal>
ISA      add
addend1  three
addend2  =arg2
sum      nil
```

==>

```
+retrieval>
ISA      order
first    three
=goal>
sum      three
count    zero
```

```
(P increment-sum
=goal>
ISA      add
sum      three
count    =count
=retrieval>
```

```
ISA      order
first    three
second   four
```

==>

```
=goal>
sum      four
+retrieval>
ISA      order
first    =count
```

Retrieved chunk:

```
ISA      order
first    three
second   four
```



# Learning New Rules

```
(P initialize-add-count
=goal>
ISA      add
addend1  three
addend2  =arg2
sum      nil
```

==>

```
+retrieval>
ISA      order
first    three
=goal>
sum      three
count    zero
```

```
(P increment-sum
=goal>
ISA      add
sum      three
count    =count
=retrieval>
```

```
ISA      order
first    three
second   four
```

==>

```
=goal>
sum      four
+retrieval>
ISA      order
first    =count
```

# Learning New Rules

```
(P initialize-add-count
=goal>
ISA      add
addend1  three
addend2  =arg2
sum      nil
```

==>

```
+retrieval>
ISA      order
first    three
=goal>
sum      three
count    zero
```

```
(P increment-sum
=goal>
ISA      add
sum      three
count    =count
=retrieval>
```

```
ISA      order
first    three
second   four
```

==>

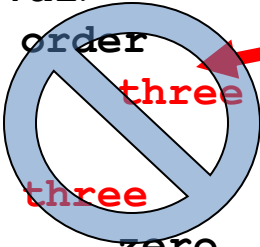
```
=goal>
sum      four
+retrieval>
ISA      order
first    =count
```

# Learning New Rules

```
(P initialize-add-count
=goal>
ISA      add
addend1  three
addend2  =arg2
sum      nil
```

==>

```
+retrieval>
ISA      order
first    three
=goal>
sum      three
count    zero
```



```
(P increment-sum
=goal>
ISA      add
sum      three
count    =count
=retrieval>
```

```
ISA      order
first    three
second   four
=goal>
sum      four
```

==>

```
+retrieval>
ISA      order
first    =count
```

# Learning New Rules

```
(P initialize-add-count
=goal>
ISA      add
addend1  three
addend2  =arg2
sum      nil
```

==>

```
+retrieval>
ISA      order
first    three
=goal>
sum      three
count    zero
```

```
(P increment-sum
=goal>
ISA      add
sum      three
count    =count
=retrieval>
```

```
ISA      order
first    three
second   four
```

==>

```
=goal>
sum      four
+retrieval>
ISA      order
first    =count
```

# Learning New Rules

```
(P initialize-add-count
=goal>
ISA      add
addend1  three
addend2  =arg2
sum      nil
```

==>

```
+retrieval>
ISA      order
first    three
=goal>
sum      three
count    zero
```

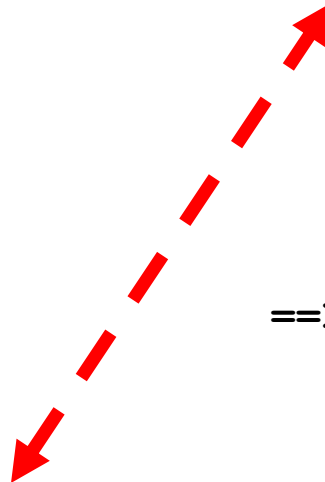
```
(P increment-sum
=goal>
ISA      add
sum      three
count    =count
```

=retrieval>

```
ISA      order
first    three
second   four
```

==>

```
=goal>
sum      four
+retrieval>
ISA      order
first    =count
```



# Learning New Rules

```
(P initialize-add-count
=goal>
ISA      add
addend1  three
addend2  =arg2
sum      nil
```

==>

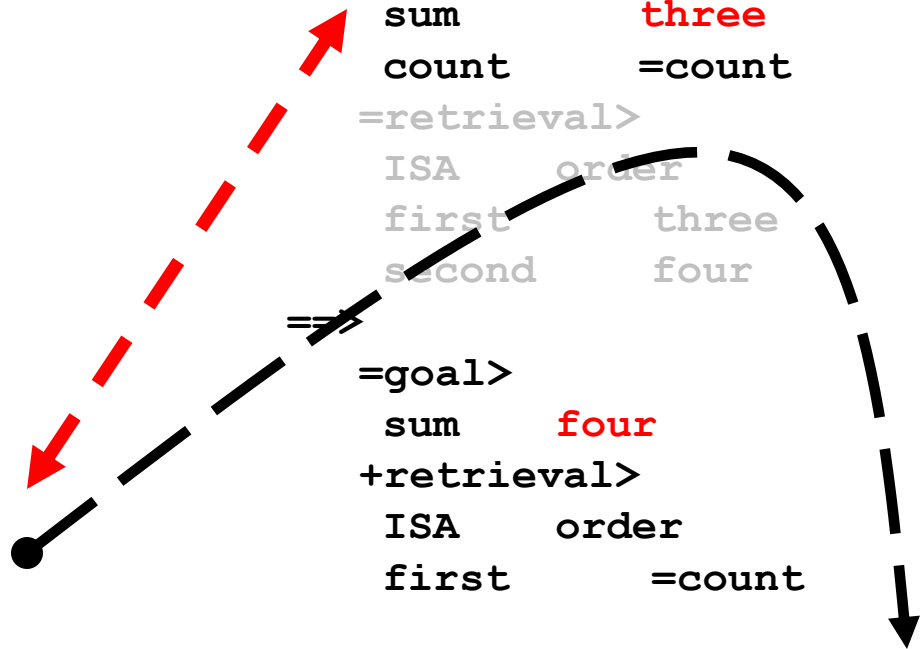
```
+retrieval>
ISA      order
first    three
=goal>
sum      three
count    zero
```

```
(P increment-sum
=goal>
ISA      add
sum      three
count    =count
```

```
=retrieval>
ISA      order
first    three
second   four
```

==>

```
=goal>
sum      four
+retrieval>
ISA      order
first    =count
```



# Learning New Rules

```
(P initialize-add-count
=goal>
ISA      add
addend1  three
addend2  =arg2
sum      nil
```

==>

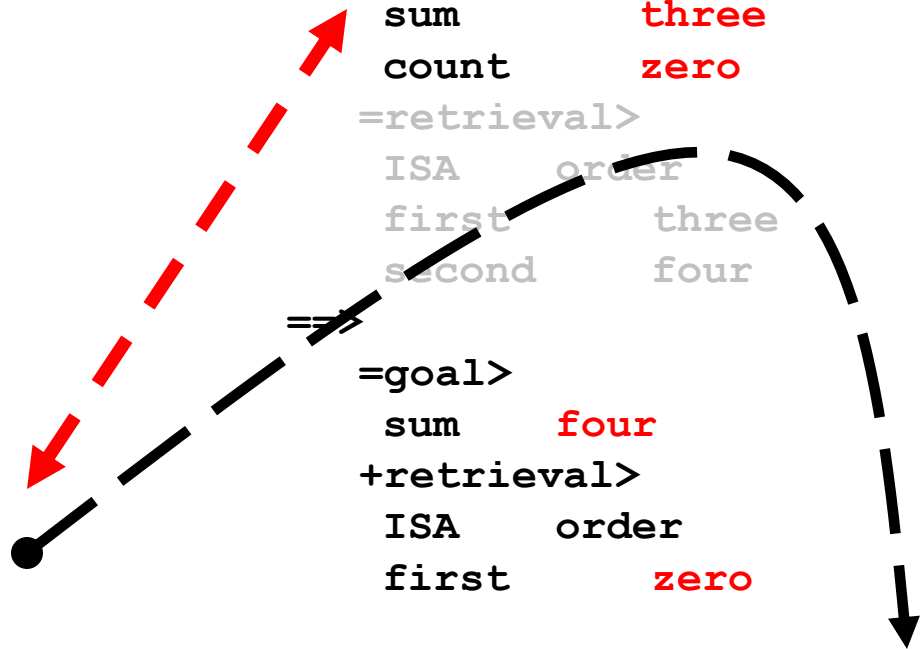
```
+retrieval>
ISA      order
first    three
=goal>
sum      three
count    zero
```

```
(P increment-sum
=goal>
ISA      add
sum      three
count    zero
```

```
=retrieval>
ISA      order
first    three
second   four
```

==>

```
=goal>
sum      four
+retrieval>
ISA      order
first    zero
```



# Learning New Rules

```
(P initialize-add-count
=goal>
ISA      add
addend1  three
addend2  =arg2
sum      nil
```

==>

```
+retrieval>
ISA      order
first    three
=goal>
sum      three
count    zero
```

```
(P increment-sum
=goal>
```

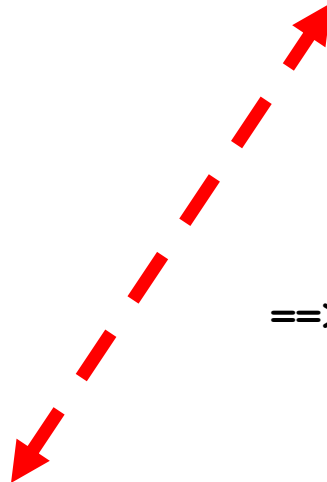
```
ISA      add
sum      three
count    zero
```

```
=retrieval>
```

```
ISA      order
first    three
second   four
```

==>

```
=goal>
sum      four
+retrieval>
ISA      order
first    zero
```





# Learning New Rules

```
(P initialize-add-count
=goal>
ISA      add
addend1  three
addend2  =arg2
sum      nil
```

==>

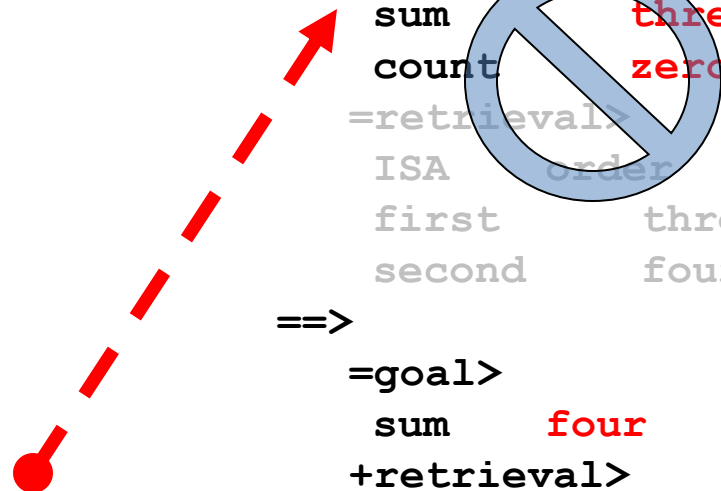
```
+retrieval>
ISA      order
first    three
=goal>
sum      three
count    zero
```

```
(P increment-sum
=goal>
```

```
ISA      add
sum      three
count    zero
=retrieval>
ISA      order
first    three
second   four
```

==>

```
=goal>
sum      four
+retrieval>
ISA      order
first    zero
```



# Learning New Rules

```
(P initialize-add-count
=goal>
ISA      add
addend1  three
addend2  =arg2
sum      nil
```

==>

```
+retrieval>
ISA      order
first    three
=goal>
sum      three
count    zero
```

```
(P increment-sum
=goal>
ISA      add
sum      three
count    zero
=retrieval>
```

```
ISA      order
first    three
second   four
```

==>

```
=goal>
sum      four
+retrieval>
ISA      order
first    zero
```

# Learning New Rules

```
(P initialize-add-count
=goal>
ISA      add
addend1  three
addend2  =arg2
sum      nil
```

==>

```
+retrieval>
ISA      order
first    three
=goal>
sum      three
count    zero
```

```
(P increment-sum
=goal>
```

```
ISA      add
sum      three
count    zero
```

```
=retrieval>
```

```
ISA      order
first    three
second   four
```

==>

```
=goal>
sum      four
+retrieval>
ISA      order
first    zero
```



# Learning New Rules

```
(P initialize-add-count
=goal>
ISA      add
addend1  three
addend2  =arg2
sum      nil
```

==>

```
+retrieval>
ISA      order
first    three
=goal>
sum      three
count    zero
```

```
(P increment-sum
=goal>
```

```
ISA      add
sum      three
count    zero
```

```
=retrieval>
```

```
ISA      order
first    three
second   four
```

==>

```
=goal>
sum      four
+retrieval>
ISA      order
first    zero
```



# Learning New Rules

```
(P initialize-add-count
=goal>
ISA      add
addend1  three
addend2  =arg2
sum      nil
```

==>

```
+retrieval>
ISA      order
first    three
=goal>
sum      three
count    zero
```

```
(P increment-sum
=goal>
ISA      add
sum      three
count    zero
=retrieval>
```

```
ISA      order
first    three
second   four
```

==>

```
=goal>
sum      four
+retrieval>
ISA      order
first    zero
```

# Learning New Rules

**LHS**

```
(P specialize-add-count  
=goal>  
ISA      add  
addend1  three  
addend2  =arg2  
sum      nil
```

```
(P increment-sum  
=goal>  
ISA      add  
sum      three  
count    zero  
=retrieval>  
ISA      order  
first    three  
second   four
```

```
=>  
+retrieval>  
ISA      order  
first    three  
=goal>  
sum      three  
count    zero
```

```
==>  
=goal>  
sum      four  
+retrieval>  
ISA      order  
first    zero
```

**RHS**

# Learning New Rules

```
(P initialize-add-count
=goal>
  ISA      add
  addend1  three
  addend2  =arg2
  sum      nil
```

==>

```
+retrieval>
  ISA      order
  first    six
=goal>
  sum      six
  count    zero
```

}

}

```
(P initialize+increment
=goal>
  ISA      add
  addend1  three
  addend2  =arg2
  sum      nil
```

==>

```
=goal>
  count    zero
  sum      four
+retrieval>
  ISA      order
  first    zero
```

```
(P increment-sum
=goal>
  ISA      add
  sum      three
  count    zero
=retrieval>
  ISA      order
  first    three
  second   four
```

==>

```
=goal>
  sum      four
+retrieval>
  ISA      order
  first    zero
```

}

# Learning New Rules

## NOTICE:

1. New rule is very specific due to adding the retrieved chunk's information to the two parent rules



# Learning New Rules

NOTICE:

2. Very simply written rules can become more sophisticated with production compilation (i.e., *write simple rules that get the desired behavior and let the system learn to be fast enough to match data...*)

# Learning New Rules

- Utility of new rule?
- Intent: gradual rule use  
(contrary to Soar philosophy)

# Learning New Rules

- Previous utility rule

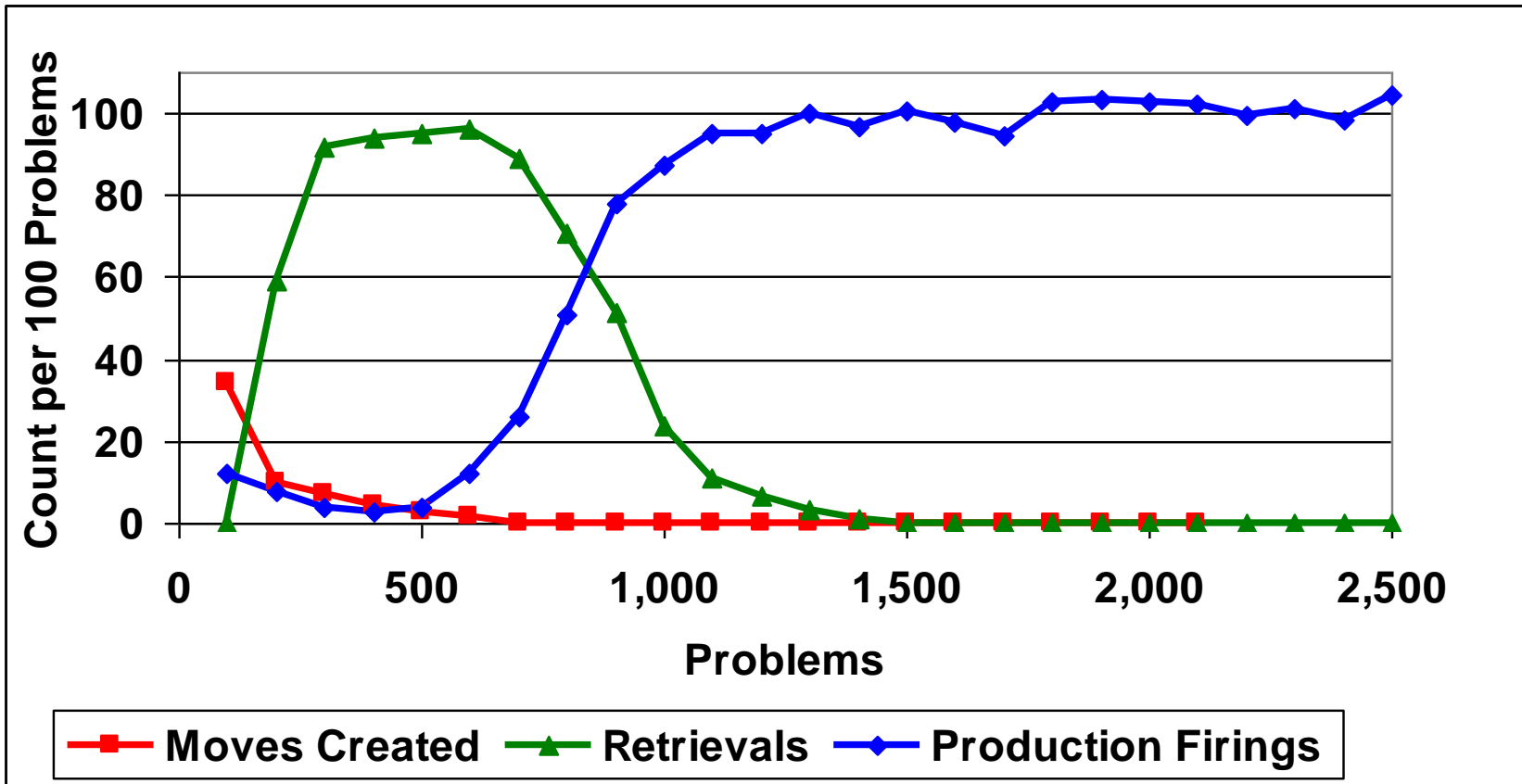
$$U_i(n) = U_i(n-1) + a [ (R_i(n) - U_i(n-1) ) ]$$

- Utility for new rule

$$U_i(n) = U_i(n-1) + a [ (U_{1st\ parent}(n) - U_i(n-1) ) ]$$

- Starts at 0 (default) and is increased with re-creation until with noise gets selected. Then gets reward more directly and can surpass parent.

# Learning New Rules



from Kennedy & Trafton (2007) Long-term Learning, CSR

# Learning New Rules

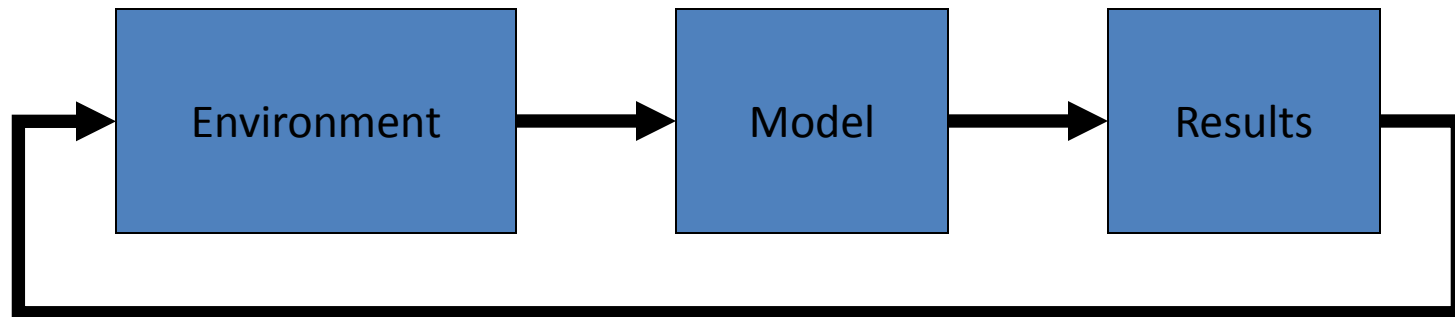
- Rule compilation conditions:
  - no conflicts
  - no “externalities”, i.e., reliance on outside world
  - must be turned on: `(sgp :ep1 t)`  
(default is nil)

# Review

- Learning new procedural knowledge:
  - 2 sequentially-firing rules combine into a new rule
  - production learning turned on with (sgp :ep1 t)
  - utility set like reward
- Use: learned new rules eventually take over and can be much faster than parents

# Unit 7 Homework

- Model design?



# Unit 7 Homework

- Given:

Regular

Irregular  
Correct

Irregular  
Incorrect



# Unit 7 Homework

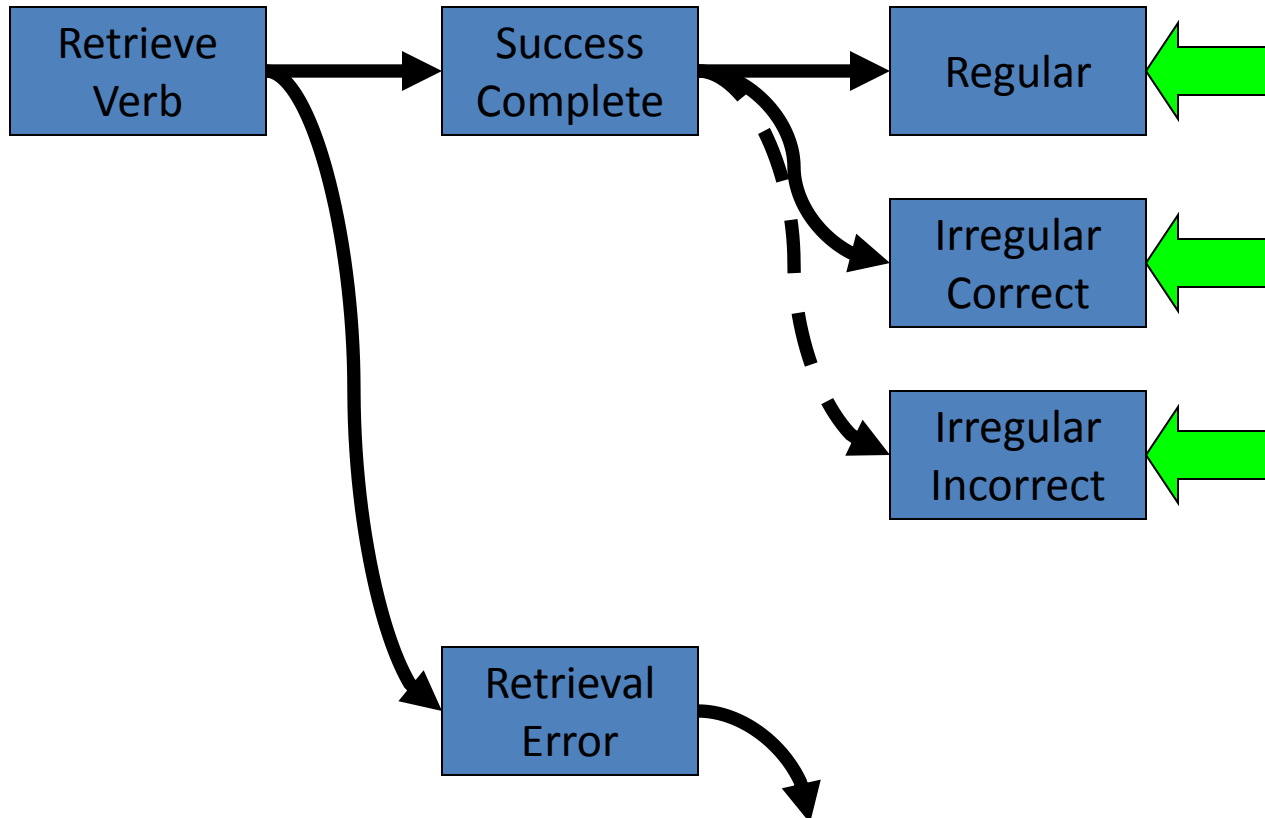
- Given:

Regular ←

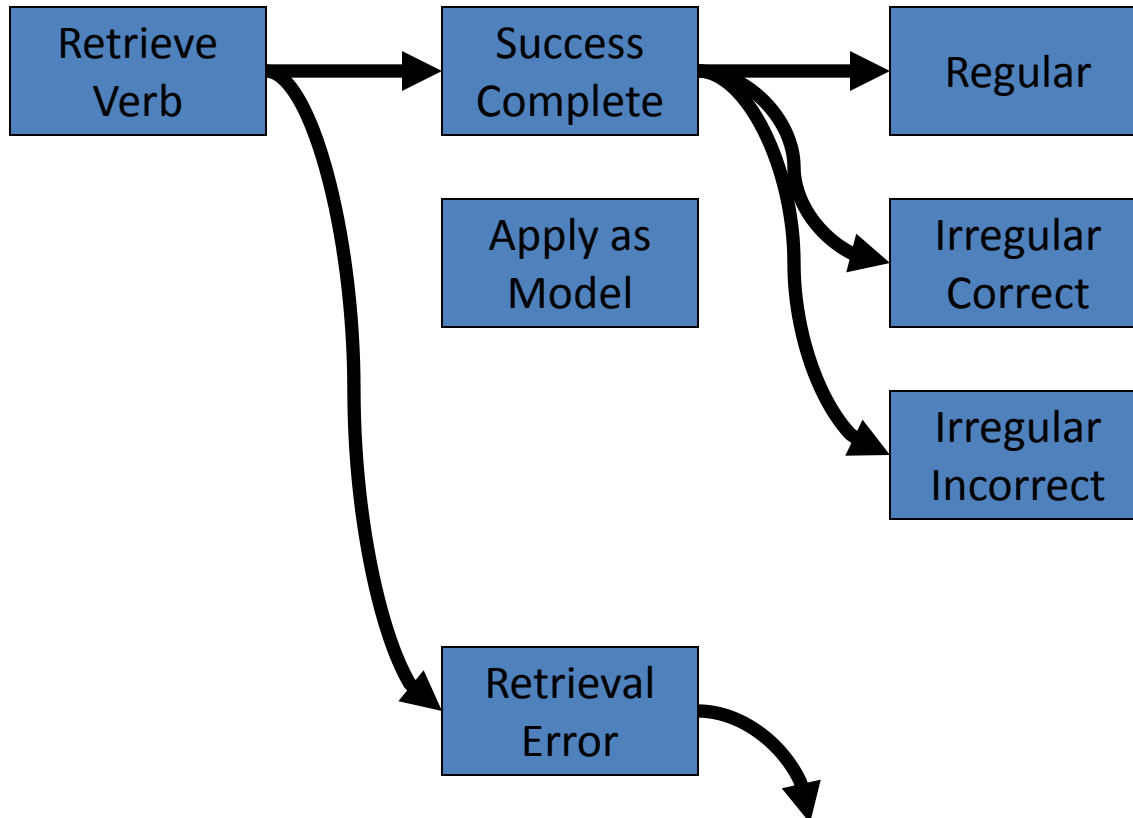
Irregular  
Correct ←

Irregular  
Incorrect ←

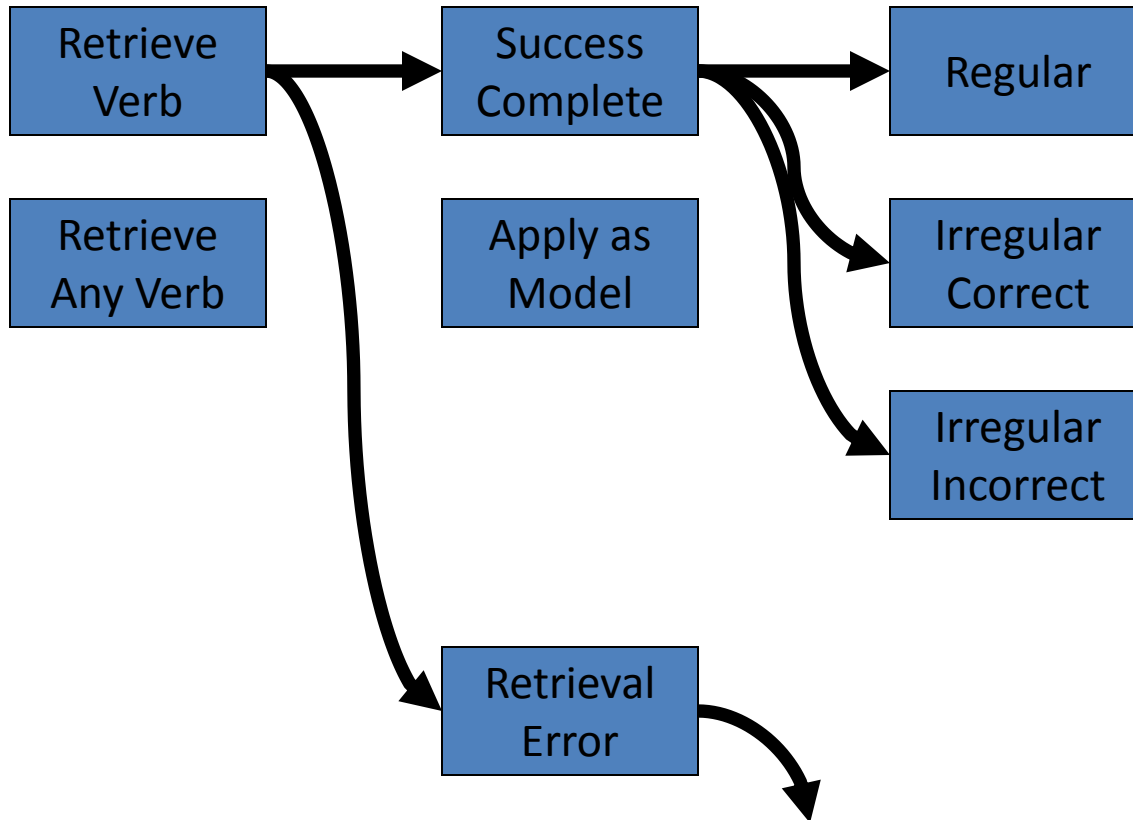
# Unit 7 Homework



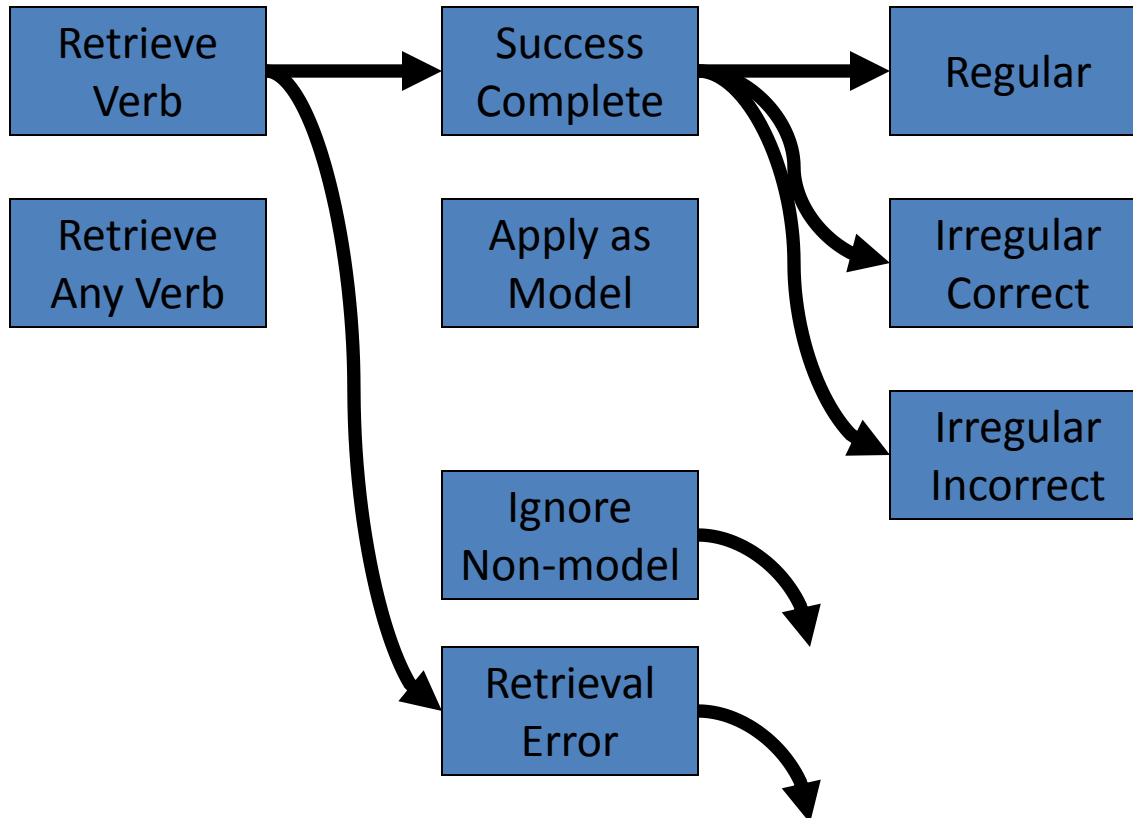
# Unit 7 Homework



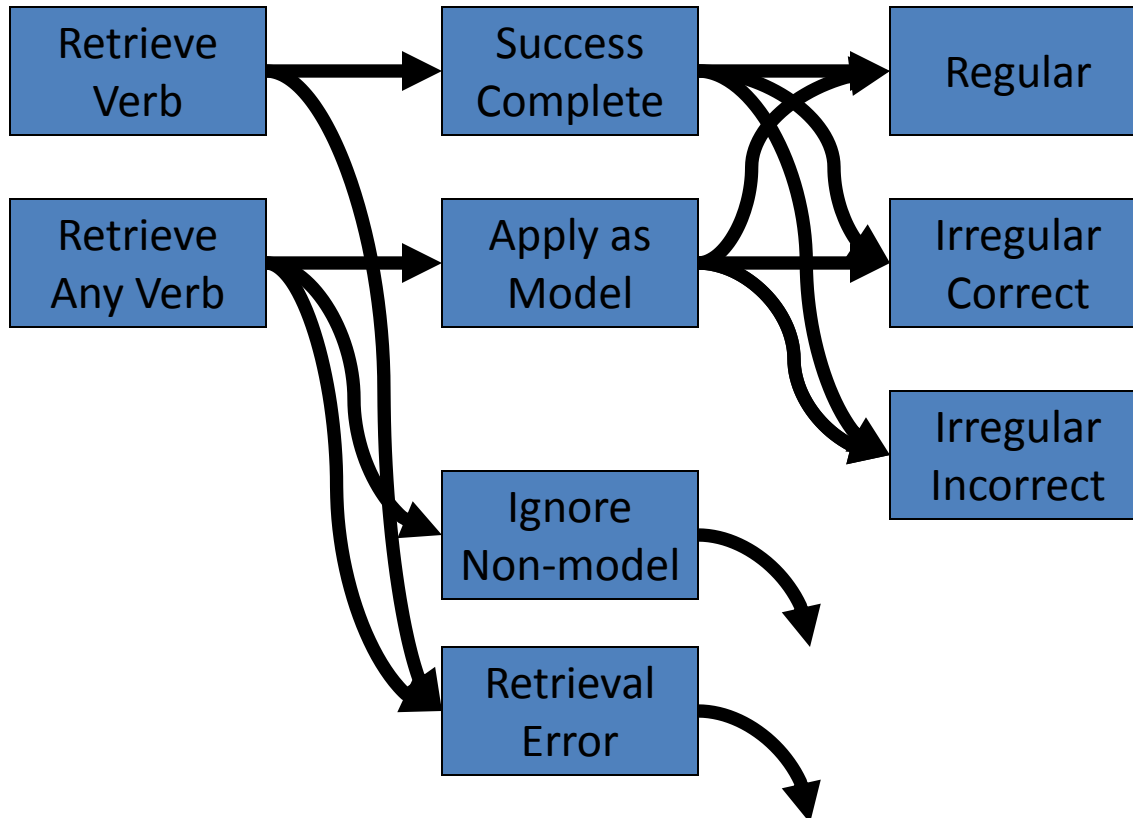
# Unit 7 Homework



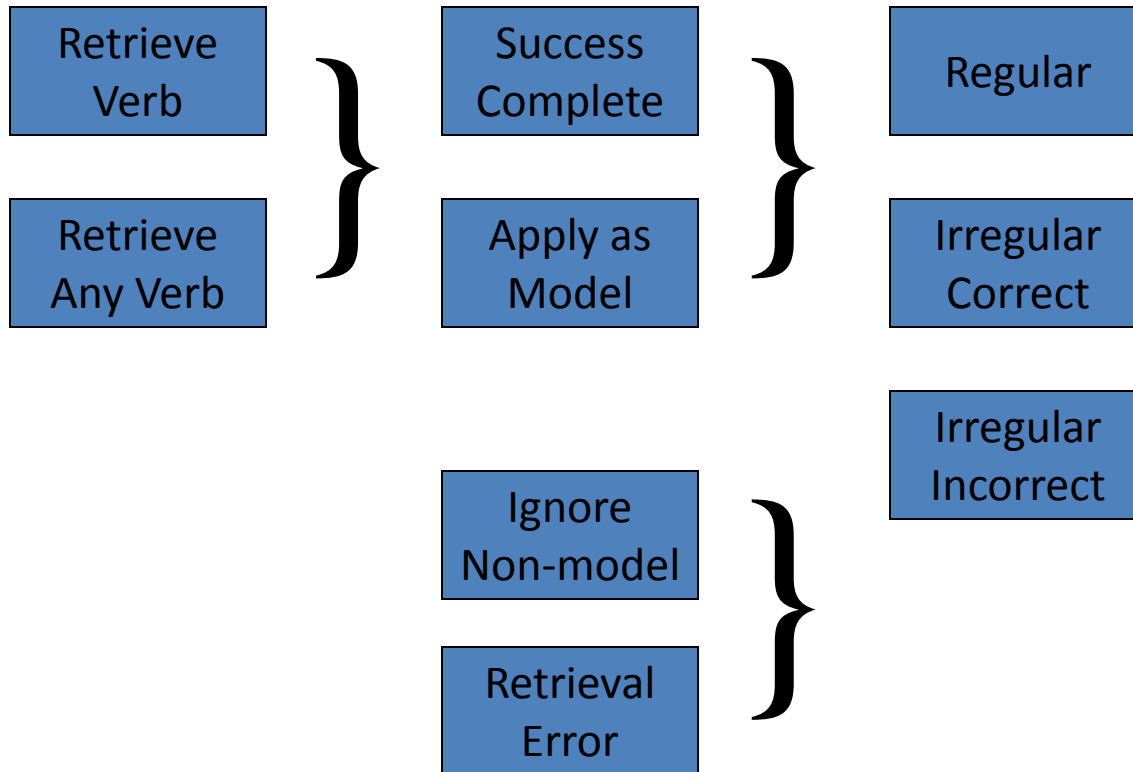
# Unit 7 Homework



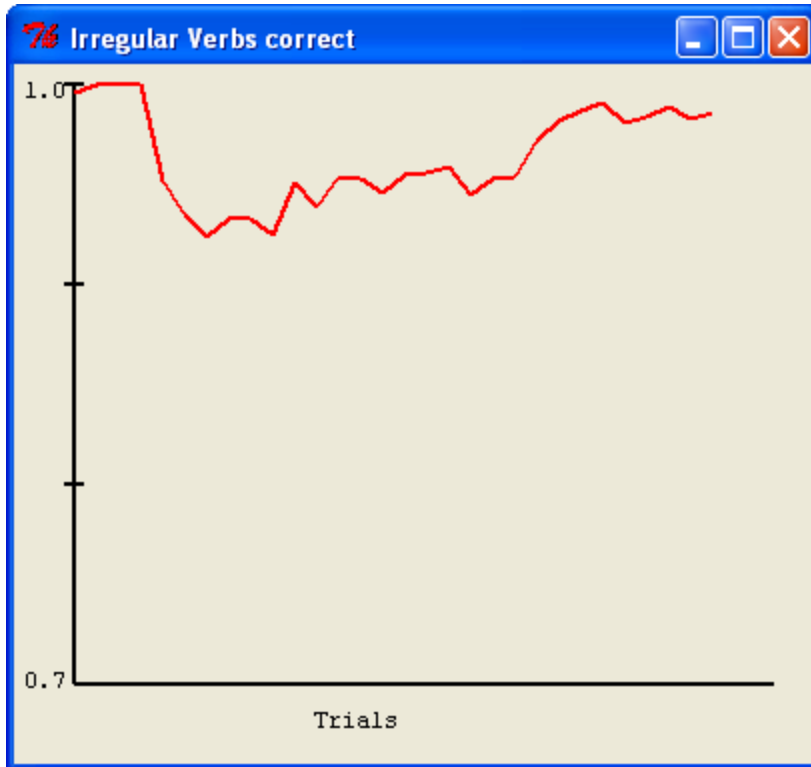
# Unit 7 Homework



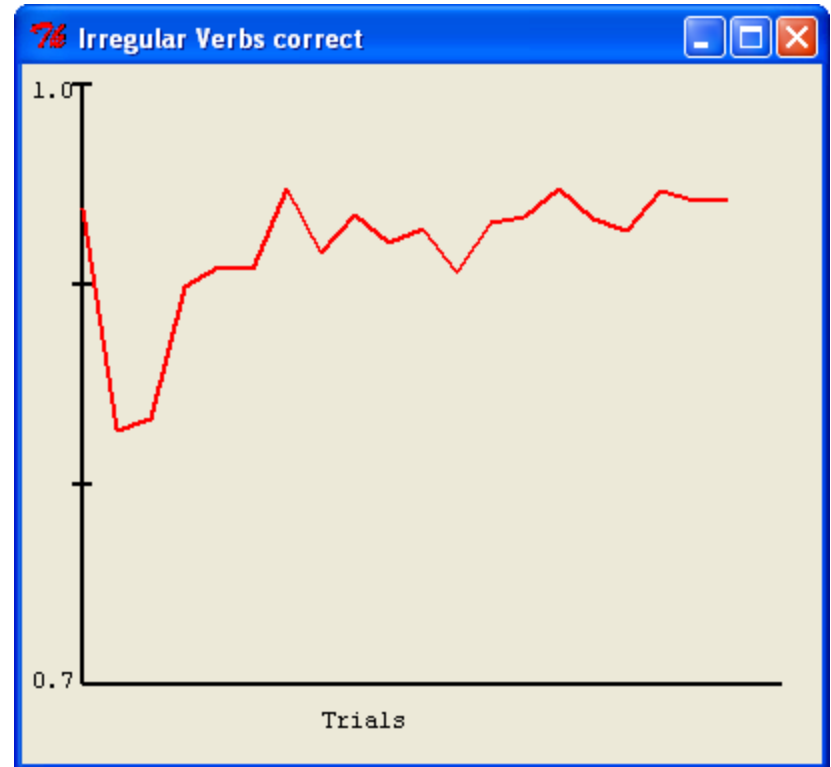
# Unit 7 Homework



# Unit 7 Homework



30,000 trials



10,000 trials 500 increment



# Issues in Cognitive Modeling

# Issues in Cognitive Modeling

- Philosophical issues
- Foundational issues
- Architectural issues
- Modeling issues
- Validation issues
- Scope issues

# Philosophical Issues

# Philosophical Issues

- Cognitive Science (& modeling) vs. Artificial Intelligence
- Sources of knowledge
- Mind-Body problem
- Computational Theory of Mind

# Philosophical Issues

- Cognitive Science (& modeling) vs Artificial Intelligence
  - similar search for understanding:
    - what is intelligence
    - how the brain produces behavior
  - different purposes
    - understanding mind for science's sake
    - applying that understanding to problems

# Philosophical Issues

- Source of knowledge
  - from experience (Locke, Hume, Mill)
  - innate, instinct, built-in (Decartes, Kant, & Pinker's "Language Instinct")

# Philosophical Issues

- Mind-body problem
  - mind distinct from body (Dualism)
  - mind an extension of the body (Materialism)
  - reality is in the mind (Idealism)

# Philosophical Issues

- Computational hypothesis
  - computation as a theory of mind
  - < 50 years old
  - John Searle's Chinese Room



# Philosophical Issues

- Symbol hypothesis
  - symbols vs. Gestalt's holistic, parallel, analog perception of whole different as from parts
  - related to neural network approach to the Cognitive Science

# Foundational Issues

# Foundational Issues

- Symbol hypothesis (on boarder)
- Levels/bands – what are we studying?
- Where is foundation
- Cognitive plausibility

# Newell's Levels & Bands

Architectural term	t (sec)	Units	System	Band
	$10^{11-13}$	$10^4$ - $10^6$ years		Evolutionary
	$10^{10}$	Millennia		Historical
Lifetime	$10^9$	~50 years		Historical
	$10^8$	Years	(Expertise)	Historical
	$10^7$	Months	(Expertise)	Social
Development	$10^6$	Weeks		Social
	$10^5$	Days		Social
	$10^4$	Hours	Task	Rational
Knowledge acq	$10^3$	10 min	Task	Rational
	$10^2$	Minutes	Task	Rational
	$10^1$	10 sec	Unit task	Cognitive
Performance	$10^0$	1 sec	Operations	Cognitive
Temp storage	$10^{-1}$	100 ms	Deliberate act	Cognitive
Primitive act	$10^{-2}$	10 ms	Neural net	Biological
	$10^{-3}$	1 ms	Neuron	Biological
	$10^{-4}$	100 $\mu$ s	Organelle	Biological

# Foundational Issues

- Where is the foundation?
  - working from neuron up
  - theory of mind down, or
  - middle in both directions

# Foundational Issues

- Cognitive plausibility
  - common usage
  - formal matching of clever experimental data
  - multi-level justification

# Architectural Issues

# Architectural Issues

- Goal of architecture
- Perception-cognition boundary
- Movement-movement boundary
- Symbolic memory representation Subsymbolic representation
- Strong assumptions



# Architectural Issues

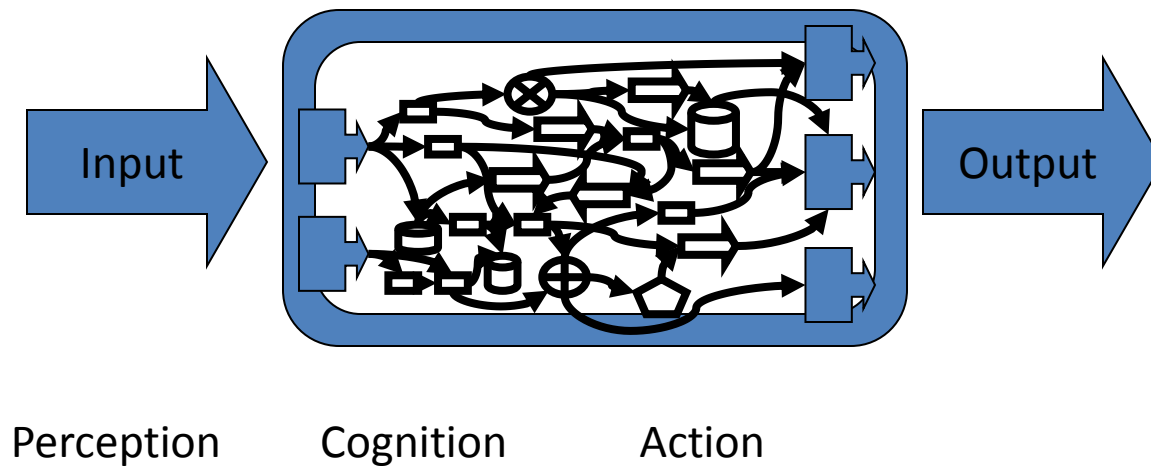
- Goal of architecture
  - AI or Cognitive Science
  - Narrow behavioral focus or broad

# Architectural Issues

- Perception-cognition boundary

# Architectural Issues

- Perception-cognition boundary



# Architectural Issues

- Perception-cognition boundary
  - where's the edge?
  - how much does one affect the other?
  - being studied

# Architectural Issues

- Movement-movement boundary
  - presumed well defined: thought vs. action
  - “Mirror neurons” challenging definition
  - not focus of study
  - (robotics not the same subject)

# Architectural Issues

- Symbolic memory representation
  - LTM & STM accepted as different
  - Procedural generally accepted as different
  - Episodic different?
  - Images different?
  - Spatial different?
  - (Feelings different?)

# Architectural Issues

- Subsymbolic representation
  - Generally accepted as necessary
  - Architectural design impact not settled
  - Neural representation?
  - Functional mathematical representation?
  - Stochastic representation?

# Architectural Issues

- Strong assumptions
  - disprovable theoretic claims to advance science
  - Newell's UTC stake in the ground
  - Icarus' variation
  - Clarion (& ACT-R) neural representation dependency
  - Modularity and physiological comparisons



# Modeling Issues

# Modeling Issues

- Standard methodologies
- Bottom-up vs. top-down
- Chunk size
- Production size
- Parameter standardization
- Other: modeling or architecture issues

# Modeling Issues

- Standard methodologies
  - Some:
    - rule based behavior
    - some patterns of rules
      - problem solving techniques
      - find, attend, harvest
      - prepare, execute
  - Lack of standard methodologies an indicator of the youth of the field or something else...

# Modeling Issues

- Bottom-up vs. top-down
  - Goal driven or environmentally driven?
  - Goal: procedural process retrieval
  - Env: perception, reactive behavior
  - Mixed? How?

# Modeling Issues

- Chunk size
  - How many slots?
    - Smaller is better
    - When is larger, too large, 7+/- 2? (!)
  - How complicated is a slot
    - indirect references?
    - variable slot names?
    - un-named slots?

# Modeling Issues

- Production size
  - How many conditions?
  - How complicated is the logic?
    - and
    - not
    - or?
    - evaluation function?
  - How many actions on RHS?
  - How complicated are the actions?

# Modeling Issues

- Parameter standardization (ACT-R)
  - Production firing: 50ms
  - Retrieval threshold: varies
  - Move attention: 85ms
  - Imaginal vs. goal buffer: ?
  - others...
- Other architectures?

# Modeling Issues

- Other: modeling or architecture issues
  - Memory for goals (are goals different?)
  - Multi-tasking (interleaved by model or architecture)
  - Emotion affecting cognition
    - different rules
    - different parameters (eg. RT)
  - Motivation(?)



# Validation Issues

# Validation Issues

- Validation criteria
- Validity vs. reliability
- Acceptable evidence

# Validation Issues

- Validation criteria
  - Statistical hypothesis testing
  - Goodness of fit
  - Verbal protocols

# Validation Issues

- Validity vs. reliability
  - Well defined phenomenon
  - Clearly demonstrated
  - Explanation rational
  - Explanation/model cognitively plausible

# Validation Issues

- How demonstrated?
  - match single human on single experiment
  - match multiple subjects on single experiment
  - match data on a wide range of behaviors
  - replicated

# Scope Issues

- Natural Language
- “Numerosity” (sense of quantity, size, etc.)
- Judgment
- Realistic vs. rational behavior
- Social behavior
- Abnormal behavior
- Creativity, art, music
- ...